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$$c_j = x_j^T \mathbf{M} x_i^*$$

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$$x_j^T \mathbf{M} x_j = 1$$

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$$\mathbf{M} \ddot{\mathbf{r}} + \mathbf{C} \dot{\mathbf{r}} + \mathbf{K} \mathbf{r} = \mathbf{p}(s, t)$$

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$\mathbf{K} \quad \mathbf{C} \quad \mathbf{M}$

$\mathbf{r}$

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$\mathbf{K}$

$\mu$

$\mathbf{K} - \mu \mathbf{M}$

$$\mathbf{p}(s, t) = \sum_j \mathbf{f}_j(s) g_j(t) = \mathbf{f}(s) \mathbf{g}(t)$$

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$\mathbf{f}_1$

$g_1(t)$

$$\mathbf{K} \mathbf{x}_1^* = \mathbf{f}_1$$

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$$\mathbf{M} \ddot{\mathbf{r}} + \mathbf{C} \dot{\mathbf{r}} + \mathbf{K} \mathbf{r} = g_1(t) \mathbf{f}_1(s)$$

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$$\mathbf{K} \mathbf{x}_i^* = \mathbf{M} \mathbf{x}_{i-1} \quad i = 2, \dots, n$$

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$$[-\omega^2 \mathbf{M} + \mathbf{K} (1 + 2\beta i)] \mathbf{r}(\omega) = G_1(\omega) \mathbf{f}_1(s)$$

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$\mathbf{r}(\omega)$

$$\mathbf{x}_i = \mathbf{x}_i^* - \sum_{j=1}^{i-1} c_j \mathbf{x}_j$$

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$$\mathbf{Y}^R \quad \mathbf{r}(\omega) = \mathbf{r}(t)e^{-i\omega t} \quad ( )$$

$$\left( \mathbf{X}^R \right)^T \quad \mathbf{g}_1(t) \quad G_1(\omega) \quad ( )$$

$$\mathbf{K}_d \mathbf{Y}^R = \mathbf{F}^R$$

$$\mathbf{C} = \frac{2\beta}{\omega} \mathbf{K}$$

$$\mathbf{K}_d = \left( \mathbf{X}^R \right)^T \left[ -\omega^2 \mathbf{M} + \mathbf{K} (1 + 2\beta i) \right] \left( \mathbf{X}^R \right) \quad ( )$$

$$\mathbf{F}^R = \left( \mathbf{X}^R \right)^T G_1(\omega) \mathbf{f}_1(s) \quad ( )$$

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$$G_1(\omega)$$

$$(G_1(\omega) = 1)$$

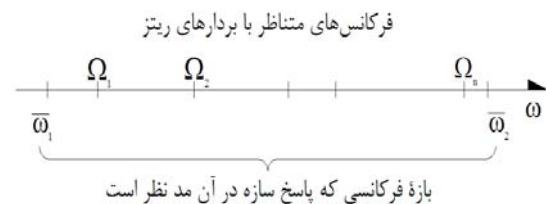
$$\left[ -\Omega_i^2 \mathbf{M} + \mathbf{K} (1 + 2\beta i) \right] \mathbf{X}_i^R = \mathbf{f}_1(s) \quad ( )$$

$$\Omega_i \quad i \quad \mathbf{X}_i^R$$

$$\mathbf{K}_d \quad ( )$$

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$\Omega_i$  :

$$\left( \left( \right) \right)$$

$$\left( \Omega_i \right)$$

$$\left( \left( \right) \right)$$

$$\mathbf{X}^R = \left[ \mathbf{X}_1^R \quad \mathbf{X}_2^R \quad \dots \quad \mathbf{X}_n^R \right] \quad ( )$$

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$$\mathbf{r} = \mathbf{X}^R \mathbf{Y}^R \quad ( )$$

$$[-\Omega_i^2 \mathbf{I} + \Lambda][\mathbf{Y}_i] = \mathbf{F} \quad (1)$$

$$[-\omega_i^2 \mathbf{M} + \mathbf{K}(1 + 2\beta i)]\mathbf{X}_i = \mathbf{0} \quad (2)$$

$$\mathbf{Y}_{ji} = \frac{\mathbf{F}_j}{-\Omega_i^2 + \omega_j^2} \quad (3)$$

$$\mathbf{X} = [\mathbf{X}_1 \quad \mathbf{X}_2 \quad \dots \quad \mathbf{X}_N] \quad (4)$$

$$\mathbf{X}_i^R = \frac{\mathbf{F}_1}{-\Omega_i^2 + \omega_1^2} \mathbf{X}_1 + \frac{\mathbf{F}_2}{-\Omega_i^2 + \omega_2^2} \mathbf{X}_2 + \dots + \frac{\mathbf{F}_N}{-\Omega_i^2 + \omega_N^2} \mathbf{X}_N \quad (5)$$

$$\Lambda = \text{Diag}[\omega_1^2 \quad \omega_2^2 \quad \dots \quad \omega_N^2] \quad (6)$$

$$\mathbf{X}^R = \mathbf{X} \mathbf{Z} \quad (7)$$

$$\mathbf{X}^T \mathbf{M} \mathbf{X} = \mathbf{I} \quad (8)$$

$$\mathbf{X}^T \mathbf{K} \mathbf{X} (1 + 2\beta i) = \Lambda \quad (9)$$

$$\mathbf{Z} = \begin{bmatrix} \frac{\mathbf{F}_1}{-\Omega_1^2 + \omega_1^2} & \frac{\mathbf{F}_1}{-\Omega_2^2 + \omega_1^2} & \dots & \frac{\mathbf{F}_1}{-\Omega_N^2 + \omega_1^2} \\ \frac{\mathbf{F}_2}{-\Omega_1^2 + \omega_2^2} & \frac{\mathbf{F}_2}{-\Omega_2^2 + \omega_2^2} & \dots & \frac{\mathbf{F}_2}{-\Omega_N^2 + \omega_2^2} \\ \vdots & \vdots & \ddots & \vdots \\ \frac{\mathbf{F}_N}{-\Omega_1^2 + \omega_N^2} & \frac{\mathbf{F}_N}{-\Omega_2^2 + \omega_N^2} & \dots & \frac{\mathbf{F}_N}{-\Omega_N^2 + \omega_N^2} \end{bmatrix} \quad (10)$$

$$[-\omega^2 \mathbf{M} + \mathbf{K}(1 + 2\beta i)]\mathbf{r}' = \mathbf{f}_1(s) \quad (11)$$

$$\mathbf{Z} = \mathbf{F}_1 \mathbf{F}_2 \dots \mathbf{F}_N \times \begin{bmatrix} \frac{1}{-\Omega_1^2 + \omega_1^2} & \frac{1}{-\Omega_2^2 + \omega_1^2} & \dots & \frac{1}{-\Omega_N^2 + \omega_1^2} \\ \frac{1}{-\Omega_1^2 + \omega_2^2} & \frac{1}{-\Omega_2^2 + \omega_2^2} & \dots & \frac{1}{-\Omega_N^2 + \omega_2^2} \\ \vdots & \vdots & \ddots & \vdots \\ \frac{1}{-\Omega_1^2 + \omega_N^2} & \frac{1}{-\Omega_2^2 + \omega_N^2} & \dots & \frac{1}{-\Omega_N^2 + \omega_N^2} \end{bmatrix} \quad (12)$$

$$[-\omega^2 \mathbf{I} + \Lambda][\mathbf{Y}] = \mathbf{F} \quad (13)$$

$$\mathbf{F} = \mathbf{X}^T \mathbf{f}_1(s) \quad (14)$$

$$\mathbf{X}_i^R = \mathbf{X}_i \quad (15)$$

$$\begin{aligned} & \underbrace{F_1 F_2 \cdots F_N}_I \times \frac{\prod_{i,j=1}^N (-\Omega_i^2 + \Omega_j^2)(\omega_i^2 - \omega_j^2)}{\prod_{i,j=1}^N (-\Omega_j^2 + \omega_i^2)} \\ & \text{Morrow Point} \quad \text{Pine Flat} \end{aligned} \tag{...}$$

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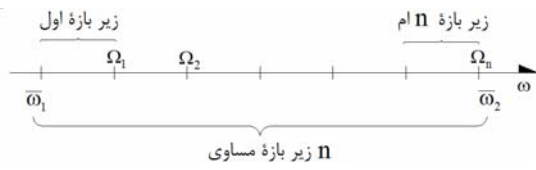
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Method II

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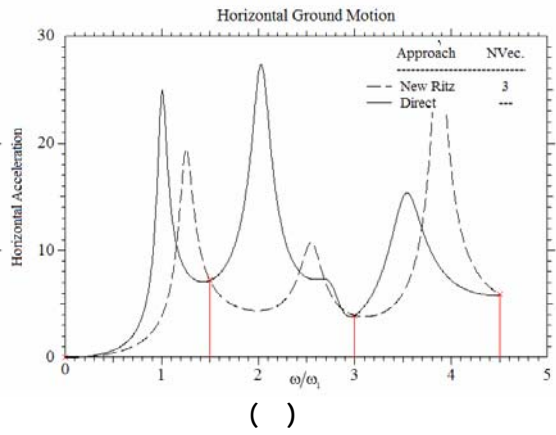
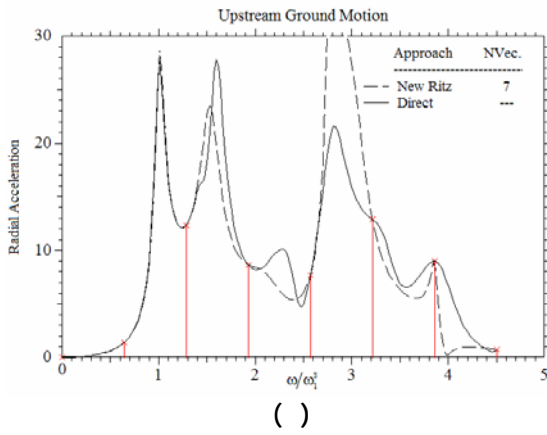
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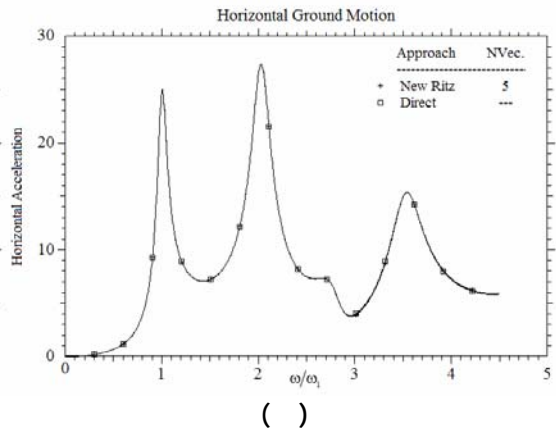
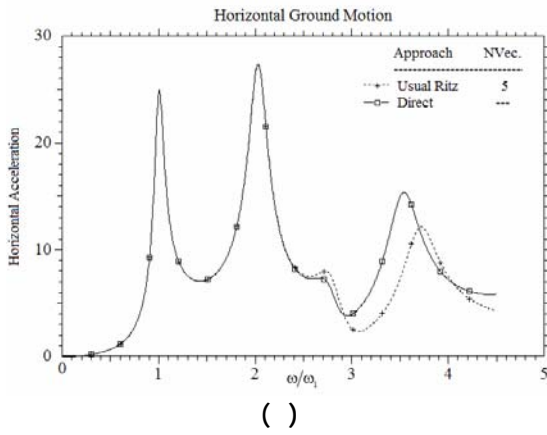


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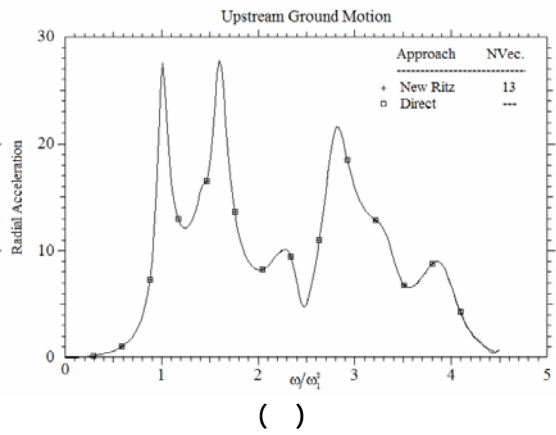
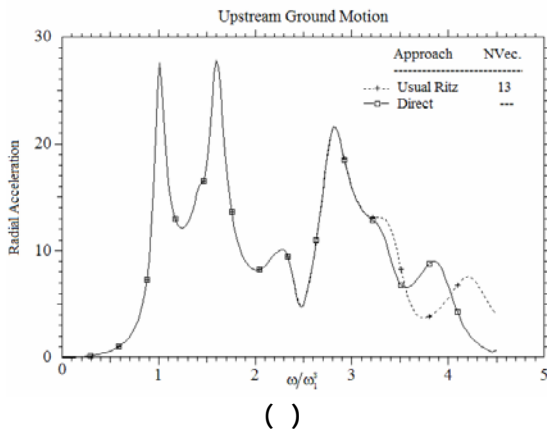
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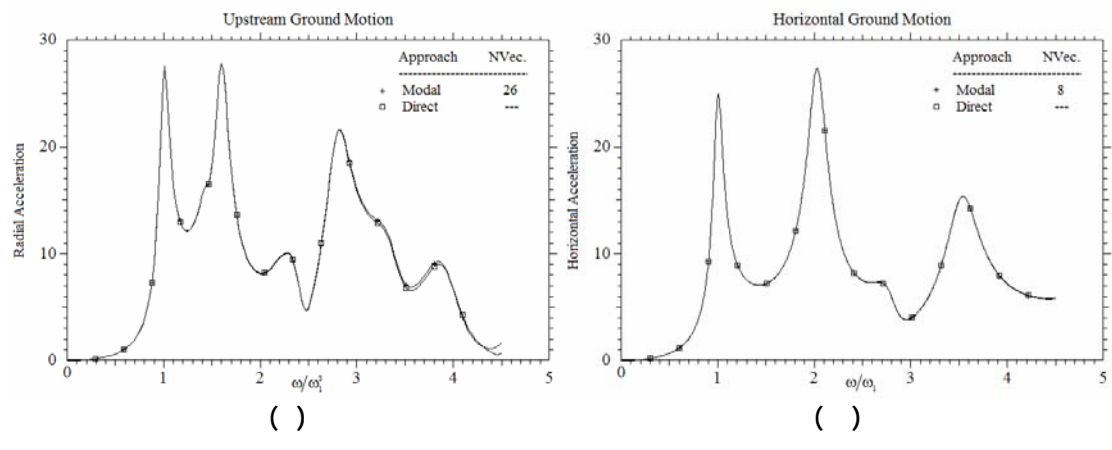


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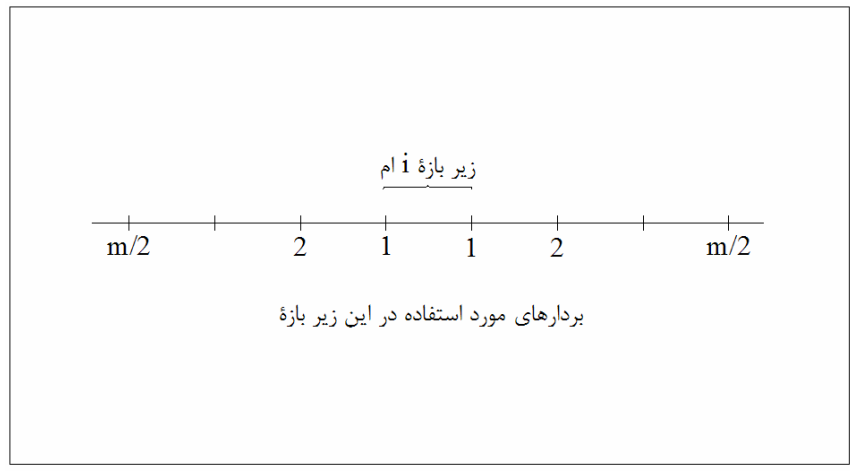
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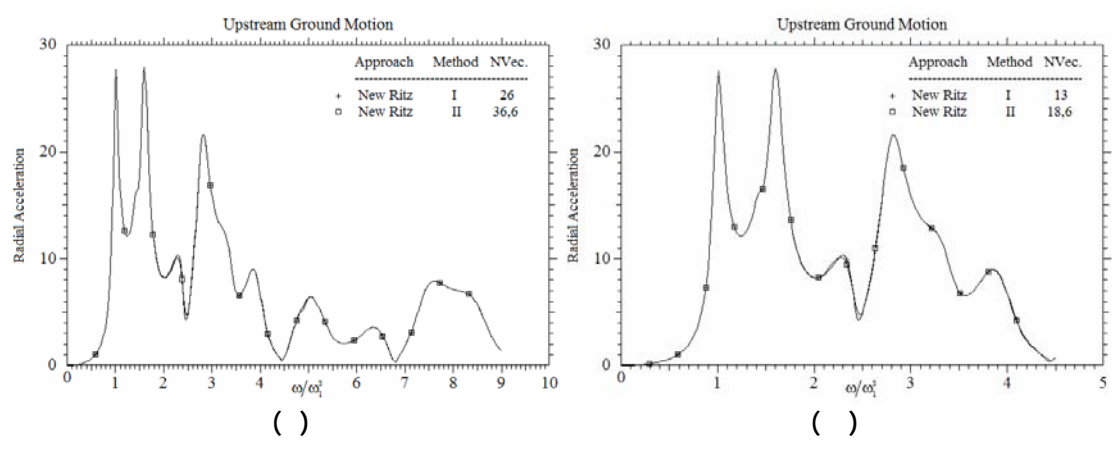




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