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$$\varepsilon_{ij} = \frac{1}{2} (u_{i,j} + u_{j,i})$$

$$E_{ijkl} = \frac{1}{2} (E_{ijkl} + E_{jikl} + E_{ijlk} + E_{jilk})$$

$$\Omega \subset \mathbb{R}^d$$

$$\Gamma = \partial\Omega$$

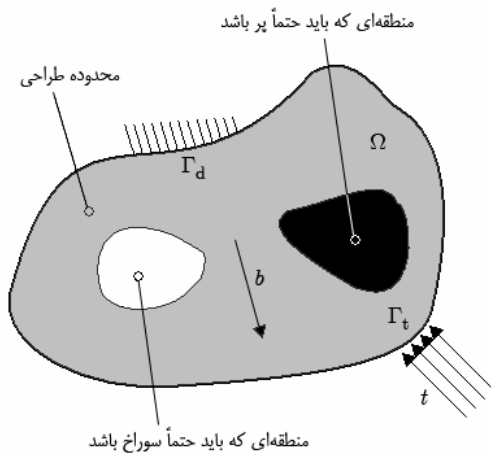
$$\Gamma = \Gamma_d \cup \Gamma_t$$

$$u_d(\mathbf{w})$$

$$(\quad)$$

$$\Omega^d \subset \Omega$$

Matlab



$$\mathbf{w} = (w_1, w_2)$$

$$: [\quad]$$

$$\min_{x(\mathbf{w}), u(\mathbf{w})} f(x, u)$$

$$\text{s.t. } a_x(u, v) = l(u), \quad \forall v \in U$$

$$g_i(x) \leq 0, \quad i = 1, \dots, m$$

$$x(\mathbf{w}) \in \{0, 1\}, \quad \forall \mathbf{w} \in \Omega^d$$

$$(\quad)$$

$$(\quad) \quad (\quad)$$

$$a_x(u, v) = l(v), \quad \forall v \in U$$

$$u(\mathbf{w}) \quad x(\mathbf{w})$$

$$U$$

$$f$$

$$g_i$$

$$\Omega^d$$

$$a_x(u, v) \quad l(u)$$

$$: [\quad]$$

$$(\quad)$$

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$$E_{ijkl}(x) = x(\mathbf{w}) E_{ijkl}^0$$

$$l(u) = \int_{\Omega} b u \, d\Omega + \int_{\Gamma_t} t u \, ds,$$

$$(\quad)$$

$$E^0$$

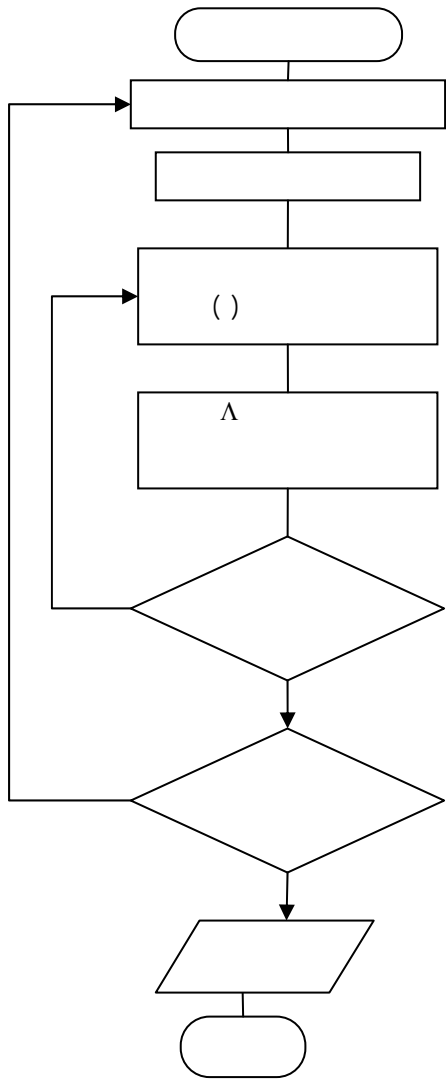
$$(\quad)$$

$$a_x(u, v) = \int_{\Omega} E_{ijkl}(x) \varepsilon_{ij}(u) \varepsilon_{kl}(v) \, d\Omega.$$

$$(\quad)$$

		SIMP	$E=E^0$		$x=1$
			$E=0$		$x=0$
	$E_{ijkl}(x) = x^p E_{ijkl}^0$			$h=0$	
				$-h \leq 0 \quad h \leq 0$	
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	:	SIMP		$x \in \{0,1\}$	
$\min_{\mathbf{x}, \mathbf{u}}$	$l(\mathbf{u}) = \mathbf{b}\mathbf{u} + \mathbf{t}\mathbf{u},$			[]	$x \in [0,1]$
s.t.	$\mathbf{K}(\mathbf{x})\mathbf{u} = \mathbf{f},$				
	$V(\mathbf{x}) = \sum_{e=1}^n x_e v_e \leq V_0,$			[]	
	$0 \leq x_e \leq 1, \quad e=1, \dots, n$			[]	
\mathbf{f}	\mathbf{u}		\mathbf{x}	()	
				()	
			\mathbf{K}		
V_0	$-e$	v_e			
			n		

$$x_e^{k+1} = \begin{cases} \max\{(1-\zeta)x_e^k, \underline{x}\} & \text{if } x_e^k (B_e^k)^\eta \leq \max\{(1-\zeta)x_e^k, \underline{x}\} \\ \min\{(1+\zeta)x_e^k, 1\} & \text{if } \min\{(1+\zeta)x_e^k, 1\} \leq x_e^k (B_e^k)^\eta \\ x_e^k (B_e^k)^\eta & \text{otherwise} \end{cases} \quad (1)$$



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$$0 \leq x \leq 1 \quad []$$

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$$0 < \underline{x} \leq x \leq 1$$

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\underline{x}

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$$\min_{\mathbf{x}, \mathbf{u}} l(\mathbf{u}) = \mathbf{t}\mathbf{u},$$

$$\text{s.t. } \mathbf{K}(\mathbf{x})\mathbf{u} = \mathbf{f},$$

$$V(\mathbf{x}) = \sum_{e=1}^n x_e v_e \leq V_0,$$

$$0 < \underline{x} \leq x_e \leq 1, \quad e=1, \dots, n$$

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:[] B_e^k

$$B_e^k = - \left(\frac{\partial l}{\partial x_e} \right)^k / \Lambda^k v_e, \quad e=1, \dots, n$$

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$$\frac{\partial l}{\partial x_e} = - p x_e^{p-1} \mathbf{u}_e^T \mathbf{K}_e \mathbf{u}_e, \quad e=1, \dots, n$$

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[-] $V=V_0$

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$$\frac{\partial l}{\partial x_e} = -\frac{p \cdot \hat{l}_e}{x_e}$$

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$$\sigma_e = \mathbf{D}_e \boldsymbol{\varepsilon}_e, \quad \mathbf{D}_e = x_e^p \mathbf{D}^0$$

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\mathbf{D}^0

$\boldsymbol{\varepsilon}_e \quad \sigma_e \quad (x=1)$

e

$$\hat{s}_j = \frac{\sum_{k \in W_j} s_{LN(j,k)}^k}{\|W_j\|}$$

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\hat{s}_j

$LN(j,k)$ j

W_j . k

W_j $\|W_j\|$

$$l(\mathbf{u}, \mathbf{x}) = \sum_{e=1}^n \int_{\Omega_e} \boldsymbol{\varepsilon}_e^T \boldsymbol{\sigma}_e(x_e) d\Omega$$

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σ_e^0 l_e . e Ω_e

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$$\sigma_e^0 = \mathbf{D}^0 \boldsymbol{\varepsilon}_e, \quad l_e = x_e^p \int_{\Omega_e} \boldsymbol{\varepsilon}_e^T \boldsymbol{\sigma}_e^0 d\Omega$$

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E=1.0

t=1.0

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$$\frac{\partial l}{\partial x_e} = \frac{\partial l_e}{\partial x_e} = -p x_e^{p-1} \int_{\Omega_e} \boldsymbol{\varepsilon}_e^T \boldsymbol{\sigma}_e^0 d\Omega$$

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$$\frac{\partial l}{\partial x_e} = -\frac{p \cdot l_e}{x_e}$$

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$$\hat{l}_e = \int_{\Omega_e} \hat{\boldsymbol{\varepsilon}}_e^T \hat{\boldsymbol{\sigma}}_e d\Omega$$

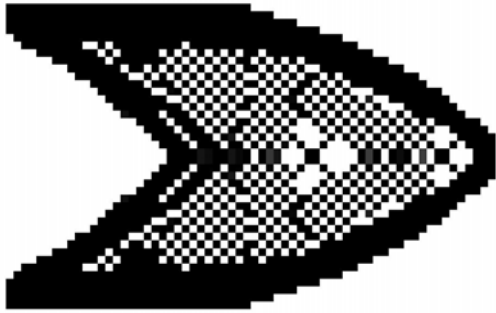
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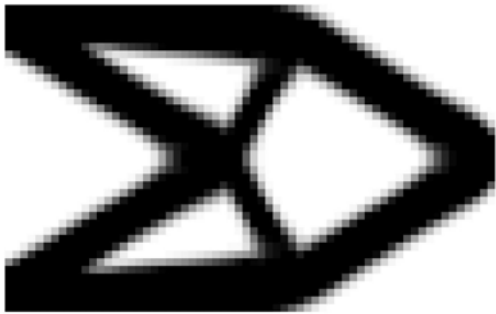
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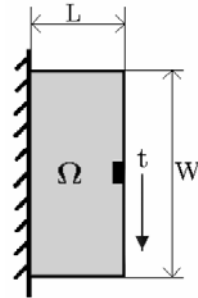
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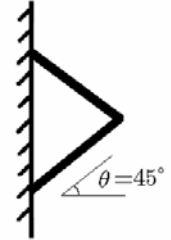
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$V_0=0.2LW$



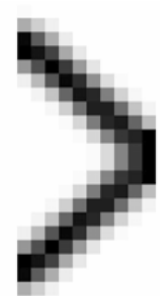
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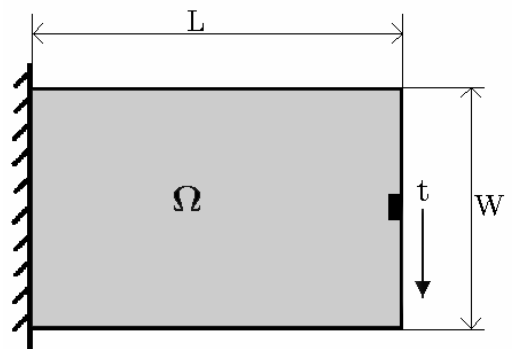
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(L=1.6W)

$V_0=0.5LW$

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$V_0=3L^2$

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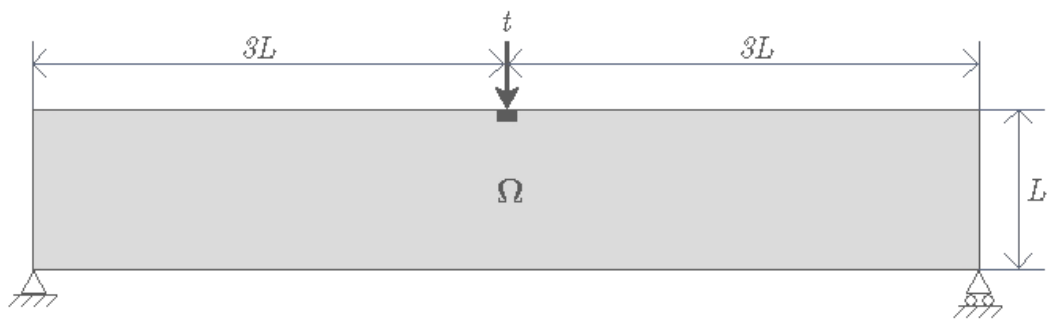
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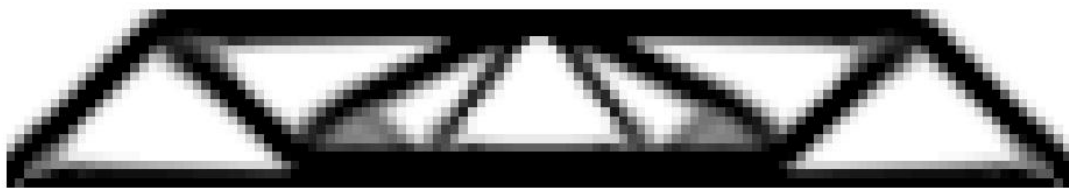
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|---|----------------------------------|
| 1 - Sizing Optimization | 19 - Global |
| 2 - Shape Optimization | 20 - Relaxed Formulation |
| 3 - Topology Optimization | 21 - Mean Compliance |
| 4 - Integrated Structural Optimization | 22 - Box Constraints |
| 5 - Homogenization | 23 - Singularity |
| 6 - Material Distribution Methods | 24 - Method of Moving Asymptotes |
| 7 - Remeshing | 25 - Optimality Criteria |
| 8 - Gray-scale Image | 26 - Kuhn-Tucker Conditions |
| 9 - Solid Isotropic Materials with Penalization | 27 - Damping Factor |
| 10 - Isotropic | |
| 11 - Design Domain | |
| 12 - The Load Linear Form | |
| 13 - The Energy Bilinear Form | |
| 14 - Weak Form | |
| 15 - Material Model | |
| 16 - Mixed | |
| 16 - Closed | |
| 18 - Lack of Continuity | |
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