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$$\tilde{\mathbf{M}}_U^T \hat{\mathbf{R}}_{n+1} = \bar{\mathbf{R}}_{n+1} + (\tilde{\mathbf{M}}_S + \tilde{\mathbf{M}}_U)(a_0 \bar{\mathbf{r}}_n + a_2 \dot{\bar{\mathbf{r}}}_n + a_3 \ddot{\bar{\mathbf{r}}}_n) + \tilde{\mathbf{C}}_S(a_1 \bar{\mathbf{r}}_n + a_4 \dot{\bar{\mathbf{r}}}_n + a_5 \ddot{\bar{\mathbf{r}}}_n) \quad ( - )$$

( )

$$a_0 = \frac{1}{\alpha \Delta t^2}, \quad a_1 = \frac{\delta}{\alpha \Delta t}, \quad a_2 = \frac{1}{\alpha \Delta t}$$

$$a_3 = \frac{1}{2\alpha} - 1, \quad a_4 = \frac{\delta}{\alpha} - 1, \quad a_5 = \Delta t \left( \frac{\delta}{2\alpha} - 1 \right) \quad ( )$$

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$$\bar{\mathbf{M}}\ddot{\bar{\mathbf{r}}} + \bar{\mathbf{C}}\dot{\bar{\mathbf{r}}} + \bar{\mathbf{K}}\bar{\mathbf{r}} = -\bar{\mathbf{M}}\bar{\mathbf{J}}\mathbf{a}_g \quad ( )$$

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$$\bar{\mathbf{M}} = \mathbf{M}_S + \mathbf{M}_U \quad ( - )$$

$$\bar{\mathbf{C}} = \mathbf{C}_S \quad ( - )$$

$$\bar{\mathbf{K}} = \mathbf{K}_S + \mathbf{K}_U \quad ( - )$$

$a_0^{-1}$

$$\mathbf{M}_S = \begin{bmatrix} \mathbf{M} & 0 \\ 0 & \frac{1}{\rho c^2} \mathbf{G} \end{bmatrix},$$

$$\mathbf{M}_U = \begin{bmatrix} 0 & 0 \\ \mathbf{B} & 0 \end{bmatrix} \quad ( - )$$

$$\mathbf{C}_S = \begin{bmatrix} \mathbf{C} & 0 \\ 0 & \frac{1}{\rho} \mathbf{L} \end{bmatrix} \quad ( - )$$

$$\mathbf{K}_S = \begin{bmatrix} \mathbf{K} & 0 \\ 0 & \frac{1}{\rho} \mathbf{H} \end{bmatrix},$$

$$\mathbf{K}_U = \begin{bmatrix} 0 & -\mathbf{B}^T \\ 0 & 0 \end{bmatrix} \quad ( - )$$

( )

$$\bar{\bar{\mathbf{M}}} = \tilde{\mathbf{M}}_S + \tilde{\mathbf{M}}_U + \tilde{\mathbf{M}}_U^T \quad ( - )$$

$$\bar{\bar{\mathbf{C}}} = \tilde{\mathbf{C}}_S \quad ( - )$$

$$\bar{\bar{\mathbf{K}}} = \tilde{\mathbf{K}}_S \quad ( - )$$

$$\hat{\mathbf{K}} = a_0 (\tilde{\mathbf{M}}_S + \tilde{\mathbf{M}}_U + \tilde{\mathbf{M}}_U^T) + a_1 \tilde{\mathbf{C}}_S + \tilde{\mathbf{K}}_S \quad ( - )$$

$$\hat{\mathbf{R}}_{n+1} = \bar{\mathbf{R}}_{n+1} + (\tilde{\mathbf{M}}_S + \tilde{\mathbf{M}}_U + \tilde{\mathbf{M}}_U^T) \hat{\mathbf{a}} (a_0 \bar{\mathbf{r}}_n + a_2 \dot{\bar{\mathbf{r}}}_n + a_3 \ddot{\bar{\mathbf{r}}}_n)$$

$$+ \tilde{\mathbf{C}}_S (a_1 \bar{\mathbf{r}}_n + a_4 \dot{\bar{\mathbf{r}}}_n + a_5 \ddot{\bar{\mathbf{r}}}_n) \quad ( - )$$

\*

$$\mathbf{K}_U = -\mathbf{M}_U^T \quad ( )$$

$$\mathbf{K}_S \mathbf{X}_i = \lambda_i \mathbf{M}_S \mathbf{X}_i \quad ( )$$

$$\mathbf{X} = \begin{bmatrix} \mathbf{X}_1 & \mathbf{0} \\ \mathbf{0} & \mathbf{X}_2 \end{bmatrix} \quad ( )$$

$\Lambda$

$$\Lambda = \begin{bmatrix} \Lambda_1 & \mathbf{0} \\ \mathbf{0} & \Lambda_2 \end{bmatrix} \quad ( )$$

$$\mathbf{X}^T \mathbf{M}_U \mathbf{X} = \begin{bmatrix} \mathbf{0} & \mathbf{0} \\ \mathbf{X}_2^T \mathbf{B} \mathbf{X}_1 & \mathbf{0} \end{bmatrix} \quad ( - )$$

$$\mathbf{X}^T \mathbf{M}_U^T \mathbf{X} = \begin{bmatrix} \mathbf{0} & \mathbf{X}_1^T \mathbf{B}^T \mathbf{X}_2 \\ \mathbf{0} & \mathbf{0} \end{bmatrix} \quad ( - )$$

$$\mathbf{C}^* = \begin{bmatrix} \mathbf{C}_1^* & \mathbf{0} \\ \mathbf{0} & \frac{1}{\rho} \mathbf{X}_2^T \mathbf{L} \mathbf{X}_2 \end{bmatrix} \quad ( - )$$

$\mathbf{C}_1^*$

$$\mathbf{C}_1^* = 2 \beta_d \Lambda_1^{1/2} \quad ( )$$

$\beta_d$

$-a_0^{-1}$

$$\hat{\mathbf{K}} = \begin{bmatrix} a_0 \mathbf{I}_1 & \mathbf{0} \\ -\mathbf{X}_2^T \mathbf{B} \mathbf{X}_1 & -\mathbf{I}_2 \end{bmatrix} + a_1 \begin{bmatrix} 2\beta_d \Lambda_1^{1/2} & \mathbf{0} \\ \mathbf{0} & -\frac{1}{\rho a_0} \mathbf{X}_2^T \mathbf{L} \mathbf{X}_2 \end{bmatrix} + \begin{bmatrix} \Lambda_1 & -\mathbf{X}_1^T \mathbf{B}^T \\ \mathbf{0} & -\frac{1}{a_0} \end{bmatrix} \quad ( )$$

$$\mathbf{X}^T \mathbf{M}_S \mathbf{X} = \mathbf{I} \quad ( - )$$

$$\mathbf{X}^T \mathbf{K}_S \mathbf{X} = \Lambda \quad ( - )$$

$( ) ( ) ( )$

$$\mathbf{X}^T \bar{\mathbf{M}} \mathbf{X} = \mathbf{I} + \mathbf{X}^T \mathbf{M}_U \mathbf{X} \quad ( - )$$

$$\mathbf{X}^T \bar{\mathbf{K}} \mathbf{X} = \Lambda - \mathbf{X}^T \mathbf{M}_U^T \mathbf{X} \quad ( - )$$

$$\bar{\mathbf{r}} = \mathbf{X} \mathbf{Y} \quad ( )$$

$\mathbf{Y}$

$$\mathbf{X}^T \quad ( )$$

$$(\mathbf{X}^T \bar{\mathbf{M}} \mathbf{X}) \ddot{\mathbf{Y}} + \mathbf{C}^* \dot{\mathbf{Y}} + (\mathbf{X}^T \bar{\mathbf{K}} \mathbf{X}) \mathbf{Y} = \mathbf{F}^*(t) \quad ( )$$

$$\mathbf{C}^* = \mathbf{X}^T \bar{\mathbf{C}} \mathbf{X} \quad ( - )$$

$$\mathbf{F}^*(t) = -\mathbf{X}^T \bar{\mathbf{M}} \bar{\mathbf{J}} \mathbf{a}_g(t) \quad ( - )$$

$( ) ( )$

$$(\mathbf{I} + \mathbf{X}^T \mathbf{M}_U \mathbf{X}) \ddot{\mathbf{Y}} + \mathbf{C}^* \dot{\mathbf{Y}} + (\Lambda - \mathbf{X}^T \mathbf{M}_U^T \mathbf{X}) \mathbf{Y} = \mathbf{F}^*(t) \quad ( )$$

$$\bar{\mathbf{K}} \quad \bar{\mathbf{M}}$$

$$\bar{\mathbf{K}}^T \mathbf{X}_i^L = \bar{\lambda}_i \bar{\mathbf{M}}^T \mathbf{X}_i^L \quad ( )$$

$$\hat{\mathbf{F}}_{n+1} = \begin{bmatrix} -\mathbf{X}_1^T \mathbf{M} \mathbf{J} \mathbf{a}_g \\ -\frac{1}{a_0} \mathbf{X}_2^T \mathbf{B} \mathbf{J} \mathbf{a} \end{bmatrix} +$$

$$\begin{bmatrix} \mathbf{I}_1 & 0 \\ -\frac{1}{a_0} \mathbf{X}_2^T \mathbf{B} \mathbf{X}_1 & -\frac{1}{a_0} \mathbf{I}_2 \end{bmatrix} (a_0 \mathbf{Y}_n + a_2 \dot{\mathbf{Y}}_n + a_3 \ddot{\mathbf{Y}}_n$$

$$\begin{bmatrix} 2\beta_d \Lambda_1^{1/2} & 0 \\ 0 & -\frac{1}{\rho a_0} \mathbf{X}_2^T \mathbf{L} \mathbf{X}_2 \end{bmatrix} (a_1 \mathbf{Y}_n + a_4 \dot{\mathbf{Y}}_n + a_5 \ddot{\mathbf{Y}}_n) \quad ( )$$

$$\mathbf{X}^R = [\mathbf{X}_1^R \quad \mathbf{X}_2^R \quad \dots \quad \mathbf{X}_m^R] \quad ( - )$$

$$\mathbf{X}^L = [\mathbf{X}_1^L \quad \mathbf{X}_2^L \quad \dots \quad \mathbf{X}_m^L] \quad ( - )$$

$$\bar{\mathbf{M}} \quad m$$

$$\begin{bmatrix} a_0 \mathbf{I}_1 + a_1 \mathbf{C}_1^* + \Lambda_1 & -\mathbf{X}_1^T \mathbf{B}^T \mathbf{X}_2 \\ -\mathbf{X}_2^T \mathbf{B} \mathbf{X}_1 & -\mathbf{I}_2 - \frac{a_1}{\rho a_0} \mathbf{X}_2^T \mathbf{L} \mathbf{X}_2 - \frac{1}{a_0} \Lambda_2 \end{bmatrix}$$

$$\begin{bmatrix} \mathbf{Y}_1 \\ \mathbf{Y}_2 \end{bmatrix}_{n+1} = \begin{bmatrix} \hat{\mathbf{F}}_1 \\ \hat{\mathbf{F}}_2 \end{bmatrix}_{n+1} \quad ( )$$

$$\bar{\mathbf{M}} \quad 1$$

$$\bar{\mathbf{K}} \quad 2$$

$$(\mathbf{X}^L)^T \bar{\mathbf{M}} \mathbf{X}^R = \mathbf{I} \quad ( - ) \quad ( )$$

$$(\mathbf{X}^L)^T \bar{\mathbf{K}} \mathbf{X}^R = \bar{\Lambda} \quad ( - ) \quad [ ]$$

$$\bar{\mathbf{K}} \mathbf{X}_i^R = \bar{\lambda}_i \bar{\mathbf{M}} \mathbf{X}_i^R \quad ( )$$

$$\bar{\mathbf{K}} \quad \bar{\mathbf{M}}$$

$$\mathbf{Y}_1 = \mathbf{M} \mathbf{V}_1 \quad ( )$$

$$k = 1, 2, \dots$$

$$\bar{\mathbf{K}} \bar{\mathbf{X}}_{k+1}^R = \mathbf{Y}_k \quad ( - )$$

$$\bar{\mathbf{Y}}_{k+1} = \mathbf{M} \bar{\mathbf{X}}_{k+1}^R \quad ( - )$$

$$\bar{\mathbf{K}} = \begin{bmatrix} \mathbf{K} & -\mathbf{B}^T \\ \mathbf{0} & \frac{1}{\rho} \mathbf{H} \end{bmatrix} \quad ( - )$$

$$\bar{\mathbf{M}} = \begin{bmatrix} \mathbf{M} & \mathbf{0} \\ \mathbf{B} & \frac{1}{\rho c^2} \mathbf{G} \end{bmatrix} \quad ( - )$$

$$\mathbf{X}_i^R$$

$$\bar{\mathbf{K}} = \mathbf{K} - \lambda_0 \mathbf{M}$$

( )

$$\rho(\bar{\mathbf{X}}_{k+1}^R) = \frac{(\bar{\mathbf{X}}_{k+1}^R)^T \mathbf{Y}_k}{(\bar{\mathbf{X}}_{k+1}^R)^T \bar{\mathbf{Y}}_{k+1}} \quad ( - )$$

( )

$$\mathbf{Y}_{k+1} = \frac{\bar{\mathbf{Y}}_{k+1}}{\left( (\bar{\mathbf{X}}_{k+1}^R)^T \bar{\mathbf{Y}}_{k+1} \right)^{1/2}} \quad ( - )$$

( )

$\lambda_0$

:

$$\rho(\bar{\mathbf{X}}_{k+1}^R) = \lambda_i \quad ( - )$$

)

$$\mathbf{X}_i = \frac{\bar{\mathbf{X}}_{k+1}^R}{\left( (\bar{\mathbf{X}}_{k+1}^R)^T \bar{\mathbf{Y}}_{k+1} \right)^{1/2}} \quad ( - )$$

(

$\mathbf{V}_1$

$\lambda_0$

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( )  $\bar{\mathbf{K}}$   $\lambda_0$

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$\mathbf{V}_1$

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$$\mathbf{K} \mathbf{X}_i = \lambda_i \mathbf{M} \mathbf{X}_i \quad ( )$$

$-\lambda_0 \mathbf{M} \mathbf{X}_i$

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$$\bar{\mathbf{K}} \mathbf{X}_i = (\lambda_i - \lambda_0) \mathbf{M} \mathbf{X}_i \quad ( )$$

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$\bar{\mathbf{K}}$

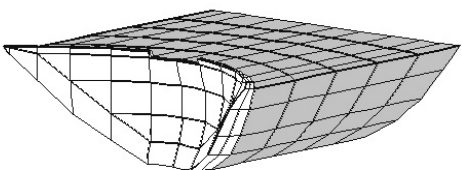
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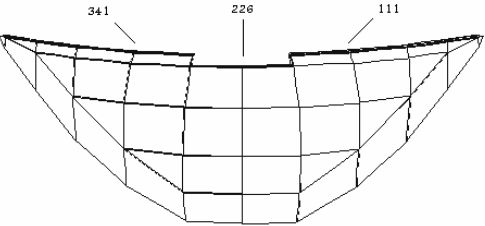
$$(\bar{\mathbf{K}}^T - \lambda_i \bar{\mathbf{M}}^T) \mathbf{X}^L = 0 \quad ( )$$

$$\bar{\mathbf{r}} = \mathbf{X}^R \bar{\mathbf{Y}} \quad ( )$$



( ) ( )

$(\mathbf{X}^L)^T$



$$\begin{aligned} & (\mathbf{X}^L)^T \bar{\mathbf{M}} \mathbf{X}^R \ddot{\bar{\mathbf{Y}}} + (\mathbf{X}^L)^T \bar{\mathbf{C}} \mathbf{X}^R \dot{\bar{\mathbf{Y}}} + \\ & (\mathbf{X}^L)^T \bar{\mathbf{K}} \mathbf{X}^R \bar{\mathbf{Y}} = -(\mathbf{X}^L)^T \bar{\mathbf{M}} \mathbf{J} \mathbf{a}_g \end{aligned} \quad ( )$$

$$\mathbf{I} \ddot{\bar{\mathbf{Y}}} + \mathbf{C}^* \dot{\bar{\mathbf{Y}}} + \mathbf{A} \bar{\mathbf{Y}} = \mathbf{F}^* \quad ( )$$

$$\begin{bmatrix} z & \text{RX} = -88 \\ \text{v} & \text{RY} = 0 \\ & \text{RZ} = 0 \end{bmatrix}$$

$$\mathbf{C}^* = (\mathbf{X}^L)^T \bar{\mathbf{C}} \mathbf{X}^R \quad ( - )$$

$$\mathbf{F}^*(t) = -(\mathbf{X}^L)^T \bar{\mathbf{M}} \mathbf{J} \mathbf{a}_g(t) \quad ( - )$$

$\bar{\mathbf{C}}$

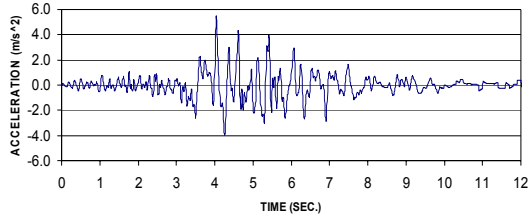
$$\bar{\mathbf{C}} = \begin{bmatrix} \alpha \mathbf{M} + \beta \mathbf{K} & \mathbf{0} \\ \mathbf{0} & \frac{1}{\rho} \mathbf{L} \end{bmatrix} \quad ( )$$

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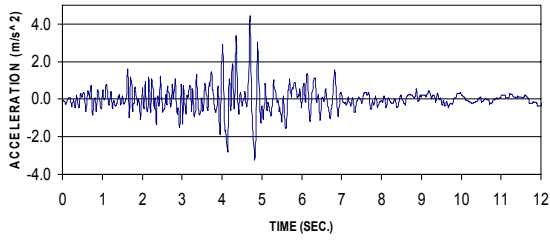
$E_c =$  GPa  
 $\gamma_c =$  kN/m<sup>3</sup>  
 $\nu_c =$  /

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kN/m<sup>3</sup>



m/s



$\beta_d =$  /

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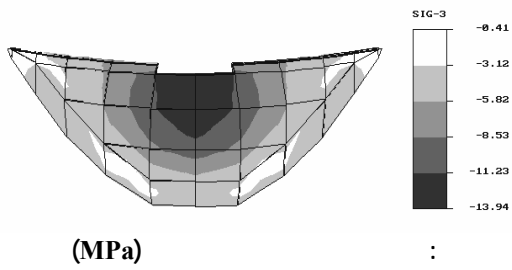
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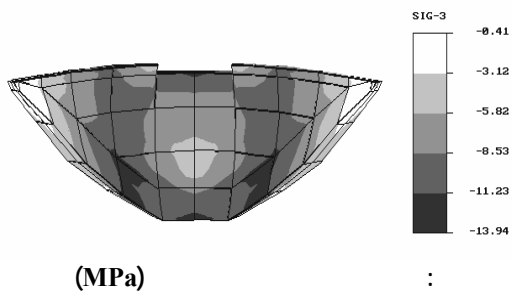
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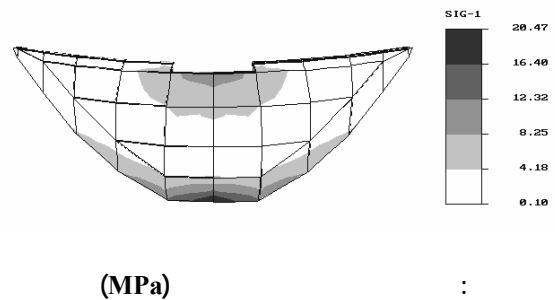
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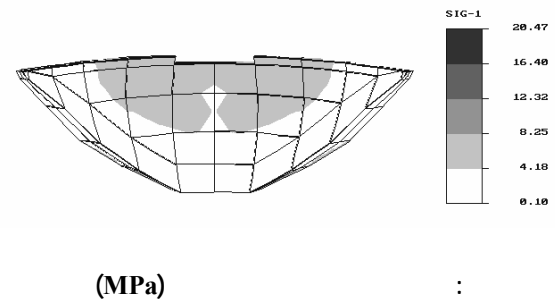
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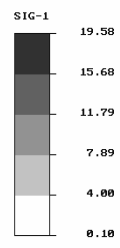
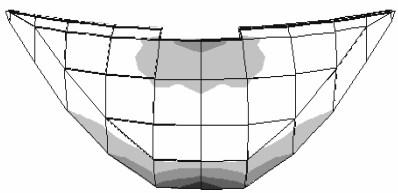
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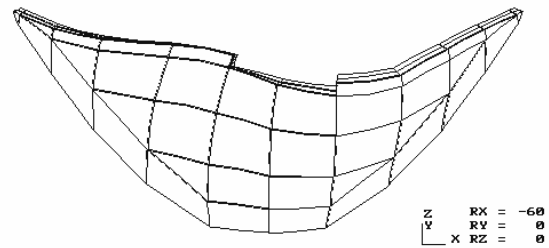
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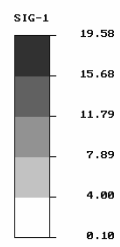
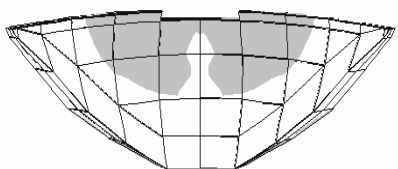
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MODE SHAPE NO. 1



Z RX = -60  
V RY = 0  
X RZ = 0

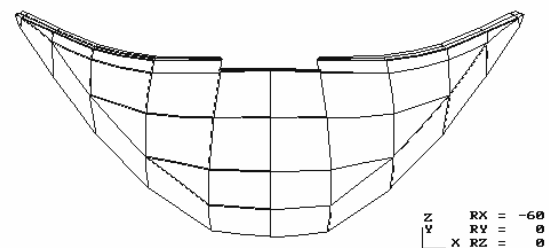
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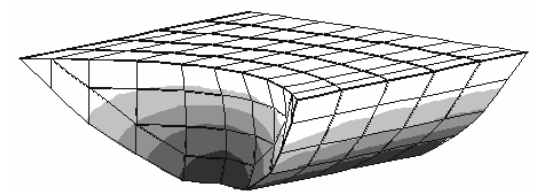
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MODE SHAPE NO. 2

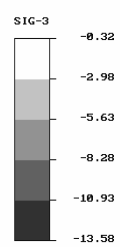
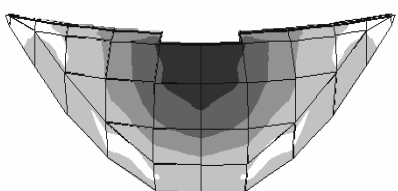


Z RX = -60  
V RY = 0  
X RZ = 0

MODE SHAPE NO. 1



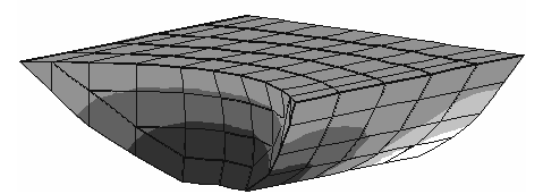
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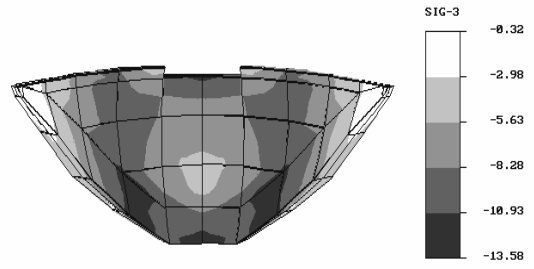
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MODE SHAPE NO. 2



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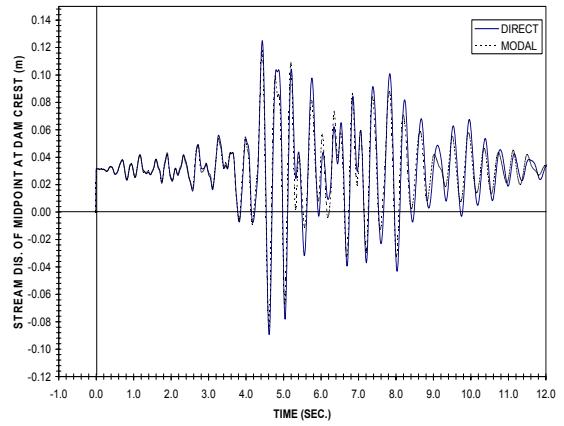


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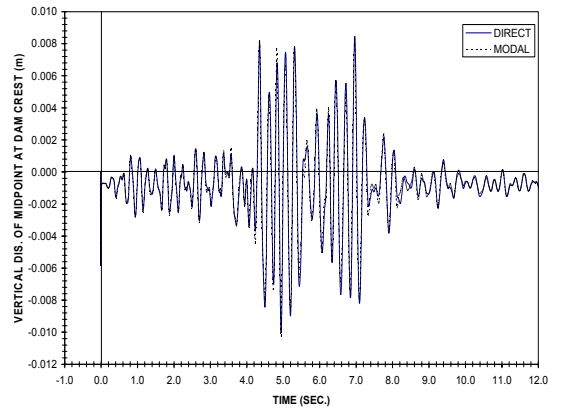
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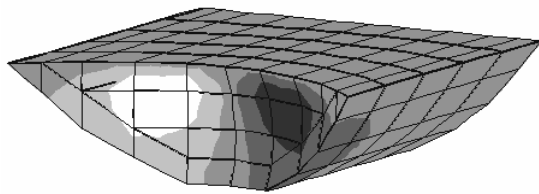
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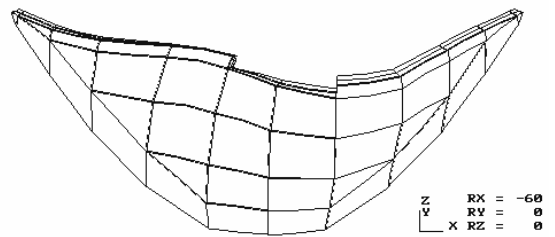
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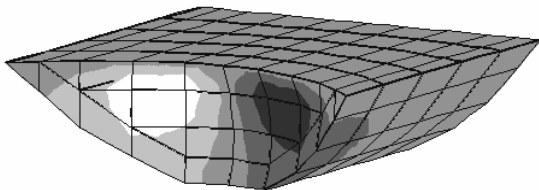
RIGHT MODE SHAPE NO. : 1



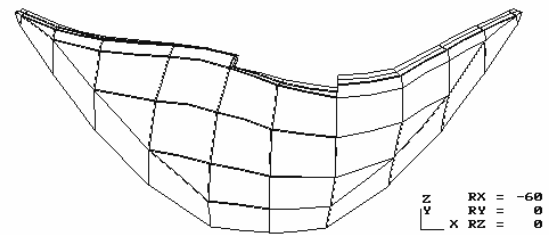
RIGHT MODE SHAPE NO. : 1



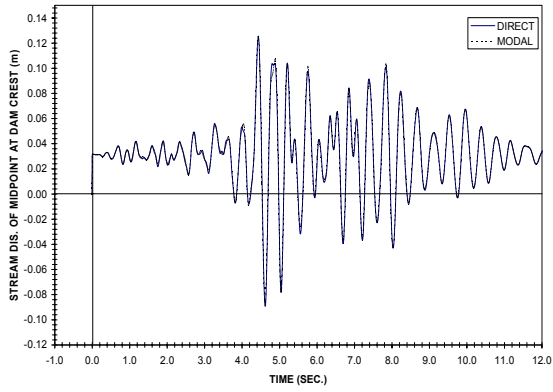
LEFT MODE SHAPE NO. : 1



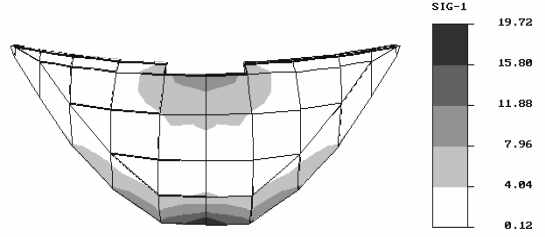
LEFT MODE SHAPE NO. : 1



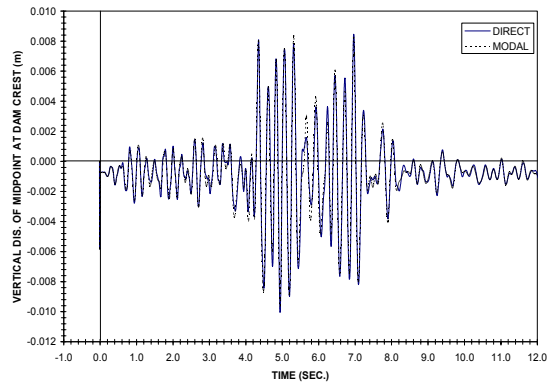
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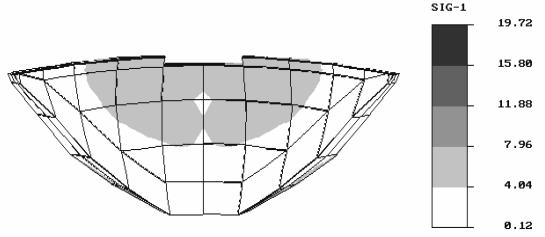
SIG-TENSION



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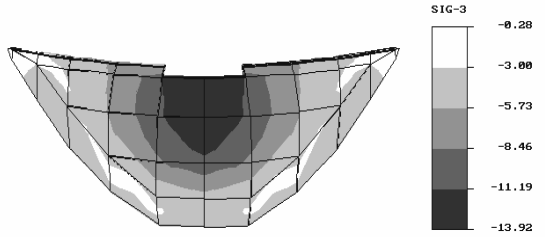


SIG-TENSION



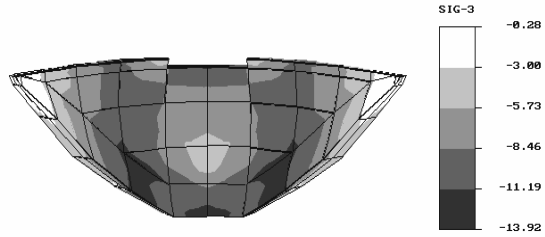
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(Skyline)

- 1 - Espandar, Radin. (1379). "*Investigation of nonlinear dynamic behavior of arch dams.*" PhD thesis, Amirkabir University of Tehran,[Persian].
  - 2 - Lotfi, V. (1376). "*Analysis of Shahid Rajaei arch dam.*" 3<sup>rd</sup> conference on large dams, Sep. 1376 [Persian].
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  - 4 - Chopra, A. K., Chakrabarti, P. and Gupta, S. (1985). *Earthquake response of concrete gravity dams including hydrodynamic and foundation interaction effects*. Report no.EERC-85/07, University of California, Berkeley US, July.
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