

Mathematical Model of Dam Reservoir Sediment Flushing by Low Level Outlet

H. M. V. Samani and A. Zaver
Civil Eng. Dept., Faculty of Engineering,
Shahid Chamran University, Ahwaz, Iran

Abstract

Sediment accumulation in reservoirs of storage dams and methods of sediment removal are significant for reservoir operation planning and increase of the dam useful life. Flushing of sediments in reservoirs is considered as one of the most important methods of sediment removal because the energy of the water flow is utilized to remove accumulated deposits. In this paper a one-dimensional mathematical model has been developed to simulate the process of sediment flushing. The model is able to predict reservoir bed profile variation during the process of flushing. The developed differential equation has been solved by the finite difference method using the control volume approach. The calibration of the model has been done by using results obtained by other researchers and then it was validated for the reservoir of Dashidaira dam. The agreement of the results obtained from the developed model has been compared with those obtained from other models.

Key words: Flushing, Finite difference, Control volume, Thomas algorithm, Boundary conditions.

()

[]

[]

[]

[]

[]

[]

[]

[]

$K - \varepsilon$

[]

[]

[]

[]

[]

[]

[]

$$(\) - \frac{\partial S}{\partial x} = -\frac{\partial^2 Z}{\partial x^2} \quad (\)$$

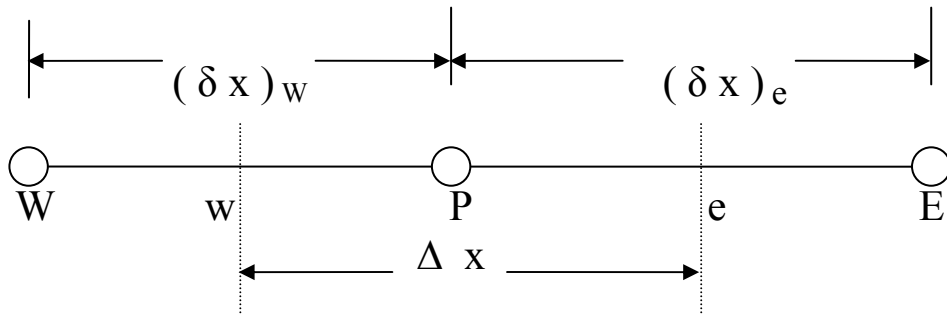
$$(\) \quad (\)$$

$$: \quad (\)$$

$$\frac{\partial Z}{\partial t} - \Gamma \frac{\partial^2 Z}{\partial x^2} = 0 \quad (\)$$

() () [] :

$$\Gamma = \frac{k_{0,q}^{0.6m+1} \cdot (3m+1)}{2(1-p)(sg-1)g^m \cdot \omega^m \cdot n^{2.4m}} \cdot S^{1.2m-1} \quad (\)$$



$$+\theta \left[\frac{\Gamma_i}{(\delta x)_e} \cdot (Z_{i+1}^{n+1} - Z_i^{n+1}) - \frac{\Gamma_i}{(\delta x)_w} \cdot (Z_i^{n+1} - Z_{i-1}^{n+1}) \right] \Delta t$$

$$= (Z_i^{n+1} - Z_i^{n+1}) \Delta x \quad (\)$$

$$\int_t^{t+\Delta t} \int_w^e \Gamma \frac{\partial^2 Z}{\partial x^2} dx dt = \int_t^{t+\Delta t} \Gamma_P \left(\frac{\partial Z}{\partial x} \right) \Big|_w^e dt$$

$$= \left[\Gamma_P \frac{Z_e - Z_P}{(\delta x)_e} - \Gamma_P \frac{Z_P - Z_w}{(\delta x)_w} \right] \Delta t \quad (\)$$

$$\frac{\Delta x}{\Delta t} = \alpha$$

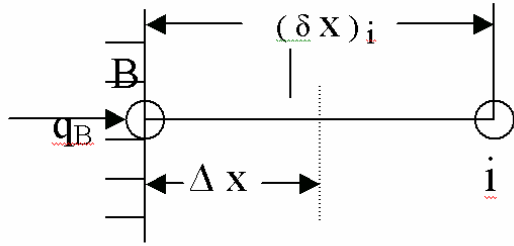
$$\int_t^{t+\Delta t} \int_w^e \frac{\partial Z}{\partial t} dx dt = \int_w^e (\Delta Z) \Big|_t^{t+\Delta t} dx = (Z_P^{n+1} - Z_P^n) \Delta x \quad (\)$$

$$(\) \quad \alpha$$

$$(\) \quad P, W, E, w, e$$

$$A_i Z_{i-1}^{n+1} + B_i Z_i^{n+1} + C_i Z_{i+1}^{n+1} = D_i \quad (\)$$

$$((1-\theta) \left[\frac{\Gamma_i}{(\delta x)_e} \cdot (Z_{i+1}^n - Z_i^n) - \frac{\Gamma_i}{(\delta x)_w} \cdot (Z_i^n - Z_{i-1}^n) \right]) \Delta t$$



$$A_i = \frac{\alpha \cdot \theta \cdot \Gamma_i}{(\delta x)_w} \quad ()$$

$$B_i = -\frac{\alpha \cdot \theta \cdot \Gamma_i}{(\delta x)_e} - \frac{\alpha \cdot \theta \cdot \Gamma_i}{(\delta x)_w} - 1 \quad ()$$

$$C_i = \frac{\alpha \cdot \theta \cdot \Gamma_i}{(\delta x)_e} \quad ()$$

$$D_i = -\alpha(1 - \theta)$$

$$\left[\frac{\Gamma_i}{(\delta x)_e} \cdot (Z_{i+1}^n - Z_i^n) - \frac{\Gamma_i}{(\delta x)_w} \cdot (Z_i^n - Z_{i-1}^n) \right] - Z_i^n \quad ()$$

$$Z = Z(0, t) \quad ()$$

()

:

$$B_n = 1, \quad A_n = 0, \quad D_n = Z(0, t), \quad C_n = 0 \quad ()$$

()

$$\Gamma_i = \frac{k_0 \cdot q^{0.6m+1} \cdot (3m + 1)}{2(1 - p)(sg - 1)g^m \cdot \omega^m \cdot n^{2.4m}}$$

$$\frac{Z - Z_{i-1}}{2\Delta x_i}^{(1.2m-1)} \quad ()$$

() () h

: ()

$$\frac{\partial Z}{\partial x} = -\left(\frac{q_s \cdot (sg - 1) \cdot g^m \cdot \omega^m \cdot n^{2.4m}}{k_0 \cdot q^{0.6m+1}} \right)^{\frac{0.833}{m}} \quad ()$$

D_s

: () ()

$$\frac{Z_2 - Z_1}{(\delta x)_c} = -\left(\frac{q_s \cdot (sg - 1) \cdot g^m \cdot \omega^m \cdot n^{2.4m}}{k_0 \cdot q^{0.6m+1}} \right)^{\frac{0.833}{m}} \quad ()$$

$$\omega = \sqrt{\frac{4gD_s}{3C_D}(sg - 1)} \quad ()$$

$$C_D = \frac{24}{R_e} + \frac{3}{\sqrt{R_e}} + 0.34 \quad ()$$

$$R_e = \frac{\rho \omega D_s}{\mu} \quad ()$$

$$C_1 = 0, \quad B_1 = 1, \quad A_1 = 0$$

$$D_1 = \left(\frac{q_s \cdot (sg - 1) \cdot g^m \cdot \omega^m \cdot n^{2.4m}}{k_0 \cdot q^{0.6m+1}} \right)^{\frac{0.833}{m}} \times \frac{(\delta x)_e}{2} \quad ()$$

...

/

$m \quad k_0$

:

$= sg$

()

$= D_s$

/

$= R_e$

/

$= \rho$

[]

/

/

/

/

[]

()

:

$$\omega = \frac{g}{18\mu} (sg - 1) \cdot D_s^2 \quad ()$$

-

()	()	()	()	()	()	
40	0.18	8.6	0.00000216	0.064	0.02	
30	0.0	9	0.0	0.1	0.00487	

$m \quad k_0$

/

[]

:

$$k_0 = 1.456 \times 10^{-6}$$

$$m = 1$$

() ()

$$D_s = 0.3mm$$

$$p = 0.4$$

$$\gamma_s = 2640 kg / m^3$$

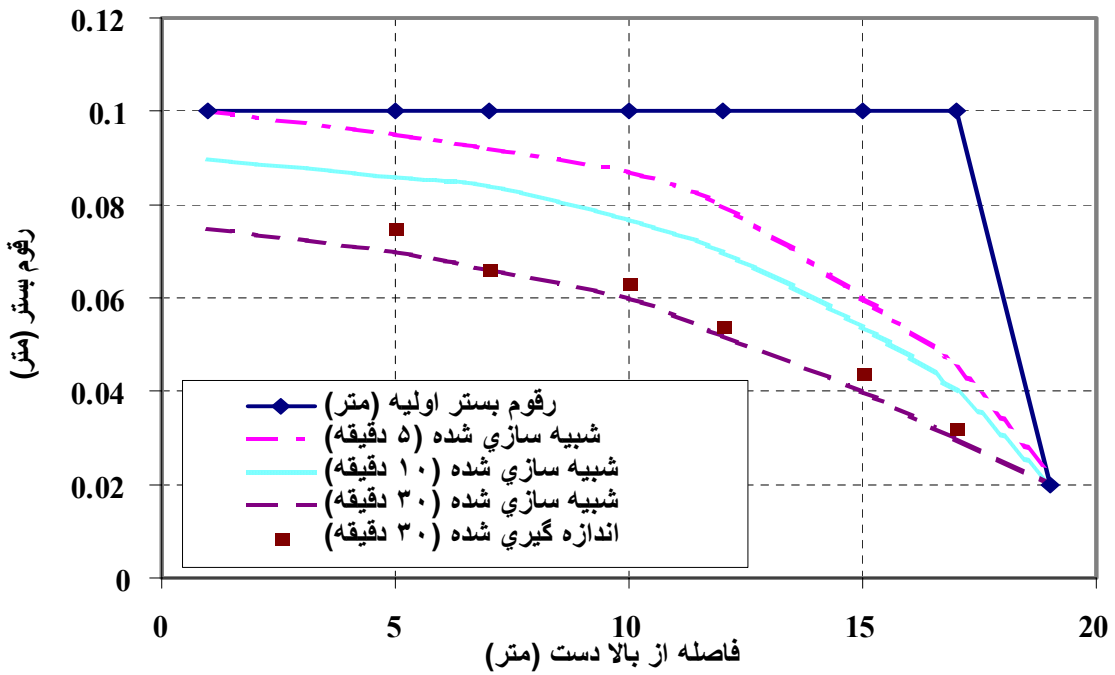
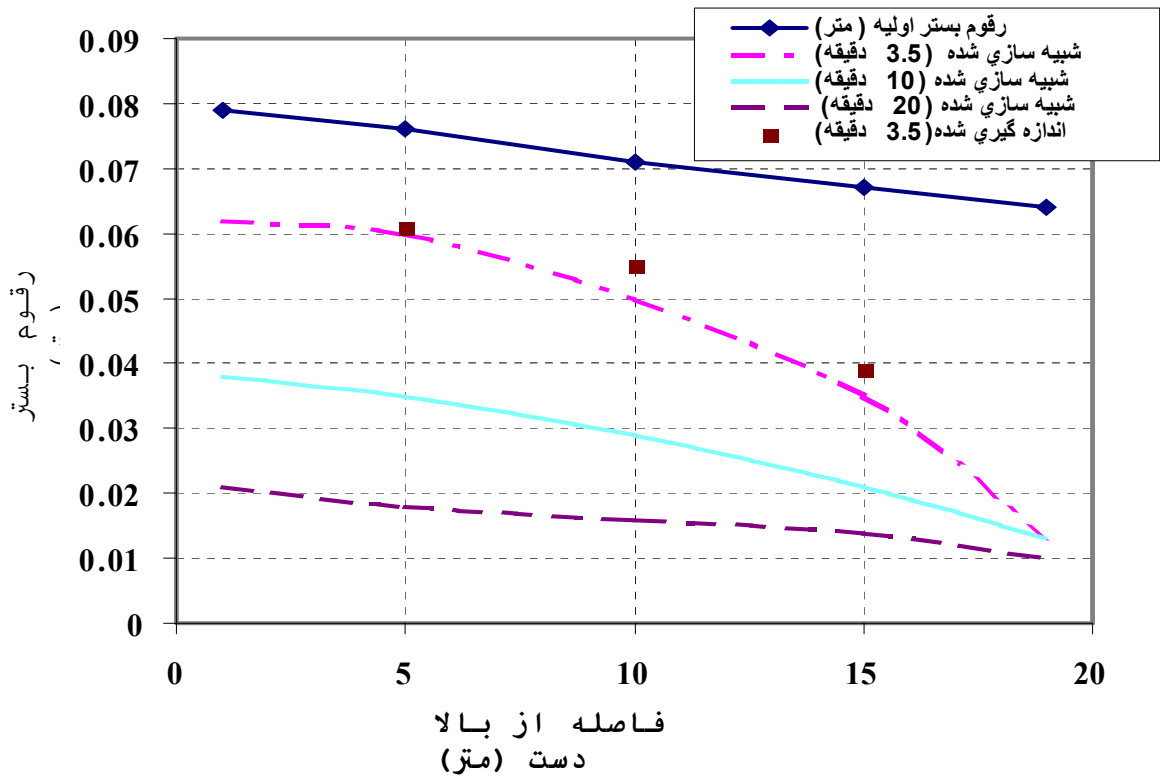
$$n = 0.03$$

$$Q = 50 m^3 / s$$

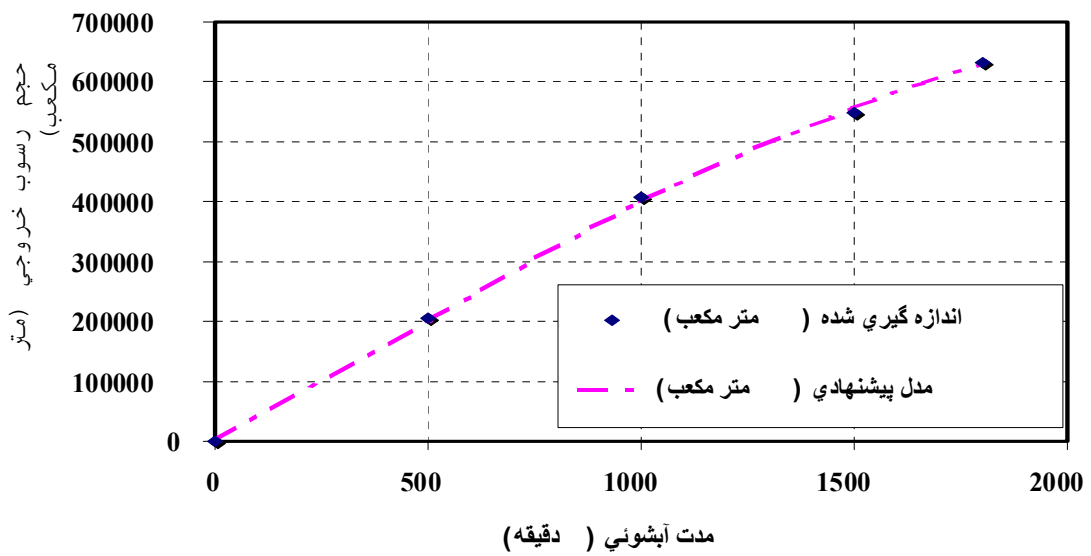
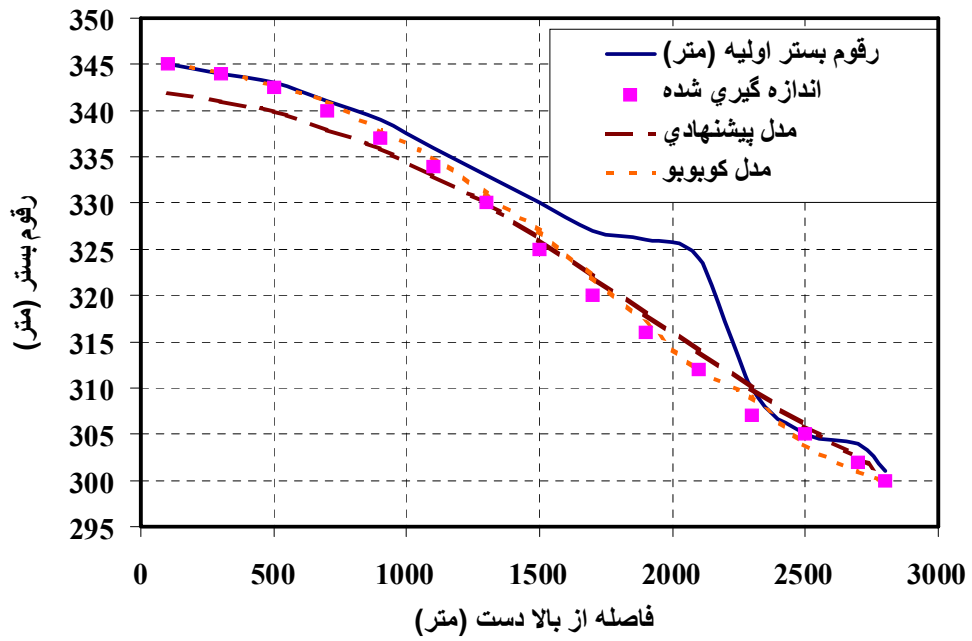
$$Z(0, t) = 29.8 m$$

$$\Delta t = 600 \text{ sec.}$$

$$\Delta x = 100 m$$



() ()



μ
 q
 q_s
 x
 T
 Δt
 θ
 Z
 u
 h
 ω
 P
 k_0
 C_D
 R_e
 S
 ρ
 D_s

-

[1] Atkinson, E. (1995), "A numerical Model for Prediction Sediment Exclusion at Intakes." Report OD 130, HR Wallingford, UK.

[2] Atkinson, E.(1996), "Flushing Sediment from Reservoirs: RESFLUSH User Manual" HR Wallingford, UK Report OD ITM 54, March.

[3] Atkinson, E. (1996), "The Feasibility of Flushing Sediment from Reservoirs." Report OD 137, Nov.

[4] Cheng, X. M. (1992), "Reservoir Sedimentaion in Chinese Hydro Schemes." Int. Water Power & Dam Construction, pp. 44-47.

[5] Fan, J., and Jiang Rujin (1980), "On Methods of Desilting of Reservoir." International Seminar of Experts on Reservoir Desilting, Tunis.

[6] Guan, Y., Rong, F., and Wang, H. (1991), "A Numerical Model for Sedimentation in Fenhe Reservoir and Adjoining Reaches." International Journal Research IRTCES, Vol. 36, No. 4, April.

[7] Hsieh, W. Shen, Jihn-Sung Lai (1996), "Flushing Sediment Through Reservoirs." Journal of Hydraulic Res. Vol 34, No.2.

γ
 sg
 g
 n

-
- [16] Scheurlein, H. (1987), "Sediment Sluicing in Mountain Reservoirs." Proc. IAHR of the Int. Workshop on Fluvial Hydraulics of Mountain Regions, Trent, Italy, Oct.3-6, pp.B77- B88.
- [17] Sen, S. P., and Srivasta (1995) "Flushing of Sediment from Small Reservoirs." Proceeding: Sixth International Symposium, River Sedimentation, New Delhi, India. C.V.J. Varma and A. R. G. Rao. Published by A. Balkema, Rotterdam.
- [18] Shen, H. W., Lai, Zhao (1993), "Hydraulic Desiltation for Non- Cohesive Sediment." In: Proc. Of the 1993 Annual ASCE Hydraulic Engineering.
- [19] Kokubo, T., Ltakura, M., Harada, M. (1997) "Predicting Methods and Actual Results on Flushing of Accumulated Deposits from Dashidaira Reservoirs" 18th. ICOLD, Q74, R.47, Florence, I Conference, San Fransisco, California, July 26-30.
- [20] Thorsten Stoesser (1999), "On the Use of A Three Dimensional. CFD Model to Simulate Reservoir Sedimentation Proccses." Proceeding.
- [21] White, W. R and Bettes, R. (1984), "The Feasibility of Flushing Sediments through Reservoirs, Proc. of the Harare Symposium. " Challenges in African Hydrology and Water Resources," July 1984. IAHR Publ. No. 144.
- [22] White, W. R . (1990), "Reservoir Sedimentation and Flushing." In: Hydrology in Regions. II- Artificial Reservoirs; Water and Slopes, Proc. Of Two Symposia, IAHR, Pub. Lusanne., No. 194, pp. 129-139.
- [8] Hsieh, W. Shen (1999), "Flushing Sediment Through Reservoirs." Journal of Hydraulic Research, Vol 37.
- [9] Ju, J. (1990), "Computational Method of Headwater Erosion and Its Application." Journal of Sediment Research, Vol.1, pp.30-39.
- [10] Jiang-Sung, Lai (1994), "Hydraulic Flushing for Reservoir Desiltation", Dissertation Presented to the University of California at Berkerly, in Partial Fulfillment of the Requirements for the Degree of Doctor of Philosophy.
- [11] Morris, G. L., and Fan, J. (1993) "Reservoir Sedimentation Handbook." McGraw Hill Book Company, pp.23.1- 23.27.
- [12] Neve, RS and Gusbi M.M., (1991) "Mathematical Modelling of Reservoir Flows In: Computer Methods in Water Resources II, Vol. 12. Computational Hydraulics and Hydrology, pp.261-269, Computational Mechanics Publications, Southampton, UK.
- [13] Olsen, N. R. B. (1991). "A Three Dimensional Numerical Model for Simulation of Sediment Movements in Water Intakes." Dissertation for the Dr. Eng. Degree, The Norwegian Institue of Technology, Division of Hydraulic Engineering, University of Trondheim.
- [14] Patankar, S. V. "Numerial Heat Transfer and Fluid Flow." Hemisphere Pub. Corp., New York: McGraw Hill.
- [15] Peng, R. and J. Niu (1987). "Numerical model for Headward Erosion on Bed Load." Journal of Sediment Research, Vol.3, Proceeding Conference IAHR, in Graz, Austria.