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In vivo

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In vitro

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¹ Invasive

⁵ Coronary artery

⁹ Distensibility

² Atherosclerosis

⁶ Carotid

¹⁰ Local pulse pressure

³ Systole

⁷ parameter

¹¹ Metabolism

⁴ Diastole

⁸ Elasticity

¹² Monitoring

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(ρ)

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$$\frac{\partial u}{\partial r} + \frac{u}{r} + \frac{\partial w}{\partial z} = 0 \quad ()$$

$$u = u(r, z, t) \quad w = w(r, z, t)$$

r z

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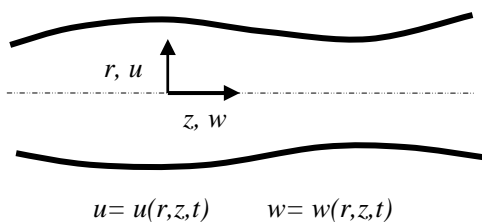
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$$\rho \left(\frac{\partial w}{\partial t} + u \frac{\partial w}{\partial r} + w \frac{\partial w}{\partial z} \right) = - \frac{\partial p}{\partial z} + \mu \left(\frac{\partial^2 w}{\partial r^2} + \frac{1}{r} \frac{\partial w}{\partial r} + \frac{\partial^2 w}{\partial z^2} \right) \quad ()$$

$$\rho \left(\frac{\partial u}{\partial t} + u \frac{\partial u}{\partial r} + w \frac{\partial u}{\partial z} \right) = - \frac{\partial p}{\partial r} + \mu \left(\frac{\partial^2 u}{\partial r^2} + \frac{1}{r} \frac{\partial u}{\partial r} + \frac{\partial^2 u}{\partial z^2} - \frac{u}{r^2} \right)$$

$$p = p(r, z, t)$$

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¹³ Hemodynamic
¹⁷ Mass conservation

¹⁴ Gradient pressure estimation
¹⁸ Momentum

¹⁵ Visual Basic
¹⁹ Navier-Stokes

¹⁶ Reynolds number

$$\frac{\partial R}{\partial z} = \tan \psi + \left(\frac{\partial R}{\partial p} \right)_z \left(\frac{\partial p}{\partial z} \right)_t \quad ()$$

$$\left(\frac{\partial R}{\partial p} \right)_z$$

(E)

[]
(C_m)

$$y = \frac{r}{R(z,t)} \quad ()$$

R(z,t)

$$c_m^2 = \frac{\bar{R}}{2\rho} \left(\frac{\partial R}{\partial p} \right)^{-1} \quad ()$$

$$c_m^2 = \frac{Eh}{2\rho \bar{R}} \quad ()$$

h

$$\left(\frac{\partial R}{\partial p} \right)_z$$

$$\frac{1}{R} \frac{\partial u}{\partial y} + \frac{u}{yR} + \frac{\partial w}{\partial z} - \frac{y}{R} \frac{\partial R}{\partial z} \frac{\partial w}{\partial y} = 0 \quad ()$$

$$\left(\frac{\partial R}{\partial p} \right)_z = \frac{\bar{R}^2}{Eh} \quad ()$$

$$\frac{\partial w}{\partial t} = -\frac{1}{\rho} \frac{\partial p}{\partial z} + \frac{1}{R} \left(yw \frac{\partial R}{\partial z} - u + y \frac{\partial R}{\partial t} \right) \frac{\partial w}{\partial y} + \frac{\mu}{\rho R^2} \left(\frac{\partial^2 w}{\partial y^2} + \frac{1}{y} \frac{\partial w}{\partial y} + R^2 \frac{\partial^2 w}{\partial z^2} \right) - w \frac{\partial w}{\partial z} \quad ()$$

$$\bar{R} = \frac{1}{T} \int_0^T R dt \quad ()$$

yR

y

T

() ()

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$$\frac{\partial R}{\partial z} = \tan \psi + \frac{\bar{R}^2}{Eh} \left(\frac{\partial p}{\partial z} \right)_t \quad (\vee \varphi)$$

$$u(y, z, t) = yw \frac{\partial R}{\partial z} - \frac{2}{y} \frac{\partial R}{\partial z} \int_0^y yw(y, z, t) dy - \frac{R}{y} \int_0^y y \frac{\partial w}{\partial z}(y, z, t) dy \quad ()$$

$$\frac{\partial R}{\partial z}$$

$$\frac{\partial R}{\partial z} = \left(\frac{\partial R}{\partial z} \right)_p + \left(\frac{\partial R}{\partial p} \right)_z \left(\frac{\partial p}{\partial z} \right)_t \quad ()$$

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(y=0)

$$\left(\frac{\partial R}{\partial z} \right)_p = \tan \psi \quad ()$$

ψ

(R) (P)

$$\sigma_2 = \frac{pR}{h}$$

:

(h)

$$\frac{\partial p}{\partial z} = \frac{-\frac{\partial w_c}{\partial t} + \frac{2w_c}{R} \left(\frac{\partial R}{\partial t} + |w_c| \tan \psi \right) + \frac{2\nu}{R^2} \left(\frac{\partial^2 w}{\partial y^2} \right)_{y=0}}{\frac{1}{\rho} - \frac{2w_c |w_c|}{R} \left(\frac{\partial R}{\partial p} \right)_z} \quad (\Delta)$$

 w_c P₀)

:

$$\frac{pR}{h} = \frac{E}{1-\nu^2} \ln\left(\frac{R}{R_0}\right) + \frac{p_0 R_0}{h_0} \quad ()$$

:

$$Rh = R_0 h_0 = cte. \quad ()$$

(R)

$$: [] \quad (\varepsilon_2)$$

:

$$p \frac{R_0(1-\nu^2)}{h_0 E} = \left(\frac{R_0}{R}\right)^2 \left(\ln \frac{R}{R_0} + \frac{p_0 R_0(1-\nu^2)}{h_0 E} \right) \quad ()$$

$$\frac{d\varepsilon_2}{dt} = \frac{1}{R} \frac{DR}{Dt} \quad ()$$

$$(\varepsilon_1) \quad (\varepsilon_2)$$

$$(\sigma_1) \quad (\sigma_2)$$

:

$$: [] \quad (\nu)$$

$$E = \frac{(R_0(1-\nu^2)/h_0) \left[p - (R_0/R)^2 p_0 \right]}{(R_0/R)^2 \ln(R/R_0)} \quad ()$$

$$\varepsilon_1 = \frac{1}{E} (\sigma_1 - \nu \sigma_2) \quad ()$$

$$\varepsilon_2 = \frac{1}{E} (\sigma_2 - \nu \sigma_1) \quad ()$$

$$E = \frac{(R_0/h_0) \left[p - (R_0/R)^2 p_0 \right]}{(R_0/R)^2 \ln(R/R_0)} \quad ()$$

E

:

$$\sigma_1 = \nu \sigma_2 \quad ()$$

:

$$\frac{1}{R} \frac{DR}{Dt} = \frac{1-\nu^2}{E} \frac{D\sigma_2}{Dt} \quad ()$$

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(A)

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$$2\sigma_2 h \Delta z = 2pR \Delta z \quad ()$$

²³ Doppler ultrasonography system
²⁷ Axial stress

²⁴ Lateral strain
²⁸ Poisson

²⁵ Axial strain
²⁹ Young modulus

²⁶ Lateral stress
³⁰ Viscoelastic

$$P = \frac{\pi R_0 h_0 E}{A} \left[\sqrt{\frac{A}{A_0}} - 1 \right] + \frac{\pi R_0 h_0 \eta}{A} \frac{1}{2\sqrt{A_0 A}} \frac{\partial A}{\partial t} + P_0 \quad ()$$

/

(/)

A_0 h_0 R_0

) P_0 P

η

E (

$$\frac{\partial R}{\partial t} \quad \frac{\partial w_c}{\partial t}$$

t

$$E = \frac{(P - P_0) - (R_0 h_0 \eta / R^2)(1/RR_0)(\partial R / \partial t)}{(R_0 h_0 / R^2)(R/R_0 - 1)} \quad ()$$

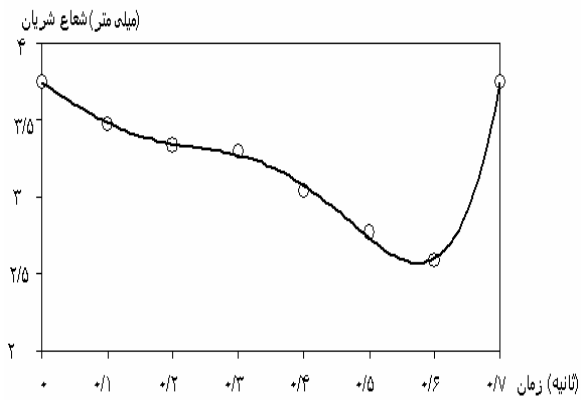
B-mode

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cm

/

/ MHz



/ s

(/ s)

³¹ Viscosity

³⁵ Mid lumen

³⁹ Microsoft Excel 2000

³² Bifurcation

³⁶ Video blaster

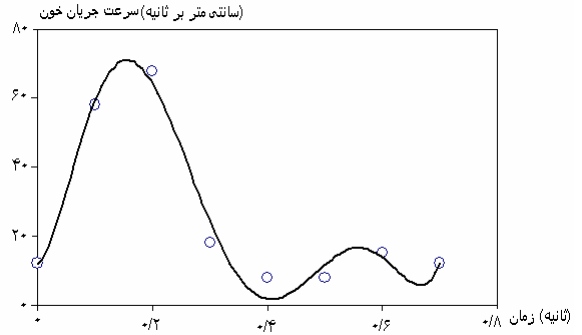
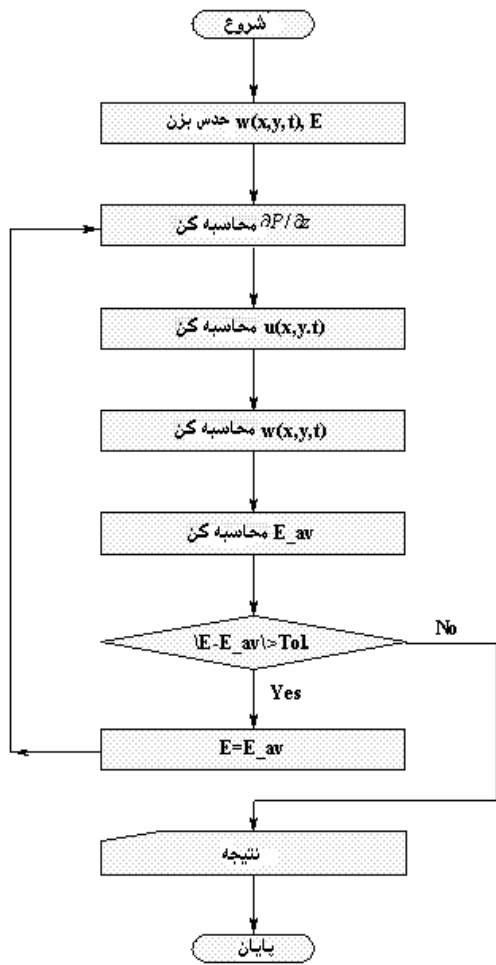
⁴⁰ Polynomial

³³ GE logic 500MD, linear array

³⁷ Real time ultrasound images

³⁴ Sample size

³⁸ B-mode



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$$\frac{\partial R}{\partial t} = R(t)$$

$$\frac{\partial w_c}{\partial t} = w_c(t)$$

[]

/ × m/s

kg/m

/ mm

[]

× Pa

/ s

[] / °

kPa

[]

Ns/m

/ s

/ mm

[]

(N/m)	
/	
/	

"

[]

:[]

MRI

$$E_p = 2E \times IMT_{D_{min}} / D_{min}$$

()

$IMT_{D_{min}}$

[]

D_{min}

()

[]

$IMT_{D_{min}}$

/ mm

() / mm

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(N/m)	
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/	

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MRI

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⁴² Peterson strain-pressure elastic modulus
⁴⁶ Non linear two dimensional model

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