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[] Tanigawa [] Noda ,

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$$MP(z) = (MP_{out} - MP_{in})V + MP_{in}$$

$$V = \left(\frac{2z+h}{2h}\right)^n \quad ()$$

$$MP_{out}, MP_{in}$$

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$$E(z) = (E_{out} - E_{in})\left(\frac{2z+h}{2h}\right)^n + E_{in}$$

$$v(z) = (v_{out} - v_{in})\left(\frac{2z+h}{2h}\right)^n + v_{in}$$

$$\alpha(z) = (\alpha_{out} - \alpha_{in})\left(\frac{2z+h}{2h}\right)^n + \alpha_{in}$$

$$\rho(z) = (\rho_{out} - \rho_{in})\left(\frac{2z+h}{2h}\right)^n + \rho_{in}$$

$$K(z) = (K_{out} - K_{in})\left(\frac{2z+h}{2h}\right)^n + K_{in} \quad ()$$

K, ρ, α, v, E

s, m

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von-Karman

$$\begin{aligned} \varepsilon_{xx} &= \frac{\partial u}{\partial x} + \frac{1}{2} \left[\left(\frac{\partial u}{\partial x}\right)^2 + \left(\frac{\partial v}{\partial x}\right)^2 + \left(\frac{\partial w}{\partial x}\right)^2 \right], \quad \varepsilon_{\theta\theta} = \frac{1}{R} \frac{\partial v}{\partial \theta} + \frac{1}{2} \left[\left(\frac{1}{R} \frac{\partial u}{\partial \theta}\right)^2 + \left(\frac{1}{R} \frac{\partial v}{\partial \theta}\right)^2 + \left(\frac{1}{R} \frac{\partial w}{\partial \theta}\right)^2 \right] + \frac{w}{R} \\ \varepsilon_{xz} &= \frac{\partial w}{\partial z} + \frac{1}{2} \left[\left(\frac{\partial u}{\partial z}\right)^2 + \left(\frac{\partial v}{\partial z}\right)^2 + \left(\frac{\partial w}{\partial z}\right)^2 \right], \quad \varepsilon_{x\theta} = \frac{1}{2} \left[\frac{1}{R} \frac{\partial u}{\partial \theta} + \frac{\partial v}{\partial x} + \frac{1}{R} \frac{\partial u}{\partial x} \frac{\partial u}{\partial \theta} + \frac{1}{R} \frac{\partial v}{\partial x} \frac{\partial v}{\partial \theta} + \frac{1}{R} \frac{\partial w}{\partial x} \frac{\partial w}{\partial \theta} \right] \\ \varepsilon_{\alpha} &= \frac{1}{2} \left[\frac{1}{R} \frac{\partial w}{\partial \theta} + \frac{\partial v}{\partial z} + \frac{1}{R} \frac{\partial u}{\partial \theta} \frac{\partial u}{\partial z} + \frac{1}{R} \frac{\partial v}{\partial \theta} \frac{\partial v}{\partial z} + \frac{1}{R} \frac{\partial w}{\partial \theta} \frac{\partial w}{\partial z} \right], \quad \varepsilon_{xz} = \frac{1}{2} \left[\frac{\partial u}{\partial z} + \frac{\partial w}{\partial x} + \frac{\partial u}{\partial x} \frac{\partial u}{\partial z} + \frac{\partial v}{\partial x} \frac{\partial v}{\partial z} + \frac{\partial w}{\partial x} \frac{\partial w}{\partial z} \right] \end{aligned} \quad ()$$

(\hat{w})

$$\varepsilon_{ij}(u, v, w) = \varepsilon_{ij}(u, v, w + \hat{w}) - \varepsilon_{ij}(0, 0, \hat{w}) \quad ()$$

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$$\begin{aligned}\varepsilon_{xx} &= \frac{\partial u}{\partial x} + \frac{1}{2} \left(\frac{\partial w}{\partial x} \right)^2 + \frac{\partial w}{\partial x} \frac{\partial \hat{w}}{\partial x}, & \varepsilon_{x\theta} &= \frac{1}{2} \left(\frac{1}{R} \frac{\partial u}{\partial \theta} + \frac{\partial v}{\partial x} + \frac{1}{R} \frac{\partial w}{\partial x} \frac{\partial w}{\partial \theta} \right) + \frac{1}{R} \frac{\partial w}{\partial x} \frac{\partial \hat{w}}{\partial \theta} + \frac{1}{R} \frac{\partial w}{\partial \theta} \frac{\partial \hat{w}}{\partial x} \\ \varepsilon_{\theta\theta} &= \frac{1}{R} \frac{\partial u}{\partial \theta} + \frac{1}{2R^2} \left(\frac{\partial w}{\partial \theta} \right)^2 + \frac{w_0}{R} + \frac{1}{R^2} \frac{\partial w}{\partial \theta} \frac{\partial \hat{w}}{\partial \theta}, & \varepsilon_{xz} &= \frac{1}{2} \left(\frac{\partial u}{\partial z} + \frac{\partial w}{\partial x} \right), & \varepsilon_{\theta z} &= \frac{1}{2} \left(\frac{\partial v}{\partial z} + \frac{1}{R} \frac{\partial w}{\partial \theta} \right), & \varepsilon_{zz} &= \frac{\partial w}{\partial z}\end{aligned}\quad ()$$

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Reddy

$$\begin{aligned}u(x, \theta, z, t) &= u_0(x, \theta, t) + z\phi_x - z^3 \frac{4}{3h^2} \left(\phi_x + \frac{\partial w_0}{\partial x} \right) \\ v(x, \theta, z, t) &= v_0(x, \theta, t) + z\phi_\theta - z^3 \frac{4}{3h^2} \left(\phi_\theta + \frac{1}{R} \frac{\partial w_0}{\partial \theta} \right) \\ w(x, \theta, z, t) &= w_0(x, \theta, t)\end{aligned}\quad ()$$

 $z = 0$ (u_0, v_0, w_0)

Von-Karman

$$\begin{array}{ccc} \phi_\theta & \phi_x & z \\ & & x \theta \end{array}\quad ()$$

$$\begin{aligned}\varepsilon_i &= \varepsilon_i^0 + z(\varepsilon_i^1 + z^2 \varepsilon_i^3) \quad \text{for } i = 1, 2, 6 \\ \varepsilon_i &= \varepsilon_i^0 + z^2 \varepsilon_i^1 \quad \text{for } i = 4, 5\end{aligned}\quad ()$$

$$\begin{aligned}\varepsilon_1^0 &= \frac{\partial u_0}{\partial x} + \frac{1}{2} \left(\frac{\partial w_0}{\partial x} \right)^2 + \frac{\partial w_0}{\partial x} \frac{\partial \hat{w}}{\partial x}, & \varepsilon_1^1 &= \frac{\partial \phi_x}{\partial x}, & \varepsilon_4^0 &= \phi_\theta + \frac{1}{R} \frac{\partial w_0}{\partial \theta} - \frac{v_0}{R} \\ \varepsilon_2^0 &= \frac{1}{R} \frac{\partial v_0}{\partial \theta} + \frac{w_0}{R} + \frac{1}{2R^2} \left(\frac{\partial w_0}{\partial \theta} \right)^2 + \frac{1}{R^2} \frac{\partial w_0}{\partial \theta} \frac{\partial \hat{w}}{\partial \theta}, & \varepsilon_2^1 &= \frac{1}{R} \frac{\partial \phi_\theta}{\partial \theta}, & \varepsilon_5^0 &= \phi_x + \frac{\partial w_0}{\partial x} \\ \varepsilon_6^0 &= \frac{\partial v_0}{\partial x} + \frac{1}{R} \frac{\partial u_0}{\partial \theta} + \frac{1}{R} \frac{\partial w_0}{\partial x} \frac{\partial w_0}{\partial \theta} + \frac{1}{R} \frac{\partial w_0}{\partial \theta} \frac{\partial \hat{w}}{\partial x} + \frac{1}{R} \frac{\partial w_0}{\partial x} \frac{\partial \hat{w}}{\partial \theta} \\ \varepsilon_6^1 &= \frac{\partial \phi_\theta}{\partial x} + \frac{1}{R} \frac{\partial \phi_x}{\partial \theta}, & \varepsilon_1^3 &= -c_2 \left(\frac{\partial \phi_x}{\partial x} + \frac{\partial^2 w_0}{\partial x^2} \right), & \varepsilon_2^3 &= -c_2 \left(\frac{1}{R} \frac{\partial \phi_\theta}{\partial \theta} + \frac{1}{R^2} \frac{\partial^2 w_0}{\partial \theta^2} - \frac{1}{R^2} \frac{\partial v_0}{\partial \theta} \right) \\ \varepsilon_4^1 &= -c_1 \left(\phi_\theta + \frac{1}{R} \frac{\partial w_0}{\partial \theta} - \frac{v_0}{R} \right), & \varepsilon_5^1 &= -c_1 \left(\phi_x + \frac{\partial w_0}{\partial x} \right) \\ \varepsilon_6^3 &= -c_2 \left(\frac{\partial \phi_\theta}{\partial x} + \frac{1}{R} \frac{\partial \phi_x}{\partial \theta} + 2 \frac{1}{R} \frac{\partial w_0}{\partial x} \frac{\partial w_0}{\partial \theta} + \frac{1}{R} \frac{\partial w_0}{\partial \theta} \frac{\partial \hat{w}}{\partial x} + \frac{1}{R} \frac{\partial w_0}{\partial x} \frac{\partial \hat{w}}{\partial \theta} - \frac{1}{R} \frac{\partial v_0}{\partial x} \right) \\ c_1 &= 4/h^2, & c_2 &= c_1/3\end{aligned}\quad ()$$

$$\delta K \int_{t_1}^{t_2} (\delta U + \delta V - \delta K) dt = 0 \quad \delta U \quad ()$$

$$\begin{aligned} \delta U &= \int_{\Omega_0} \int_{-\frac{h}{2}}^{\frac{h}{2}} \{ [\sigma_{xx} (\delta \varepsilon_{xx}^{(0)} + z \delta \varepsilon_{xx}^{(1)} - c_1 z^3 \delta \varepsilon_{xx}^{(3)}) + \sigma_{\theta\theta} (\delta \varepsilon_{\theta\theta}^{(0)} + z \delta \varepsilon_{\theta\theta}^{(1)} - c_1 z^3 \delta \varepsilon_{\theta\theta}^{(3)}) \\ &\quad + \sigma_{r\theta} (\delta \gamma_{x\theta}^{(0)} + z \delta \gamma_{x\theta}^{(1)} - c_1 z^3 \delta \gamma_{x\theta}^{(3)}) + \sigma_{xz} (\delta \gamma_{xz}^{(0)} + z^2 \delta \gamma_{xz}^{(2)}) + \sigma_{\theta z} (\delta \gamma_{\theta z}^{(0)} + z^2 \delta \gamma_{\theta z}^{(2)})] dz \} dx d\theta \\ &= \int_{\Omega_0} (N_{xx} \delta \varepsilon_{xx}^{(0)} + M_{\theta\theta} \delta \varepsilon_{\theta\theta}^{(1)} - c_1 P_{\theta\theta} \delta \varepsilon_{\theta\theta}^{(3)} + N_{\theta\theta} \delta \varepsilon_{\theta\theta}^{(0)} + M_{\theta\theta} \delta \varepsilon_{\theta\theta}^{(1)} - c_1 P_{\theta\theta} \delta \varepsilon_{\theta\theta}^{(3)} \\ &\quad + N_{x\theta} \delta \gamma_{r\theta}^{(0)} + M_{x\theta} \delta \gamma_{r\theta}^{(1)} - c_1 P_{x\theta} \delta \varepsilon_{x\theta}^{(3)} + Q_{\theta} \delta \gamma_{xz}^{(0)} - c_2 R_x \delta \gamma_{xz}^{(0)} + Q_{\theta} \delta \gamma_{\theta z}^{(0)} - c_2 R_{\theta} \delta \gamma_{\theta z}^{(0)}) dx d\theta \\ \delta V &= - \int_{\Gamma} \int_{-\frac{h}{2}}^{\frac{h}{2}} [\hat{\sigma}_{nm} (\delta u_n + z \delta \phi_n - c_1 z^3 \delta \varphi_n) + \hat{\sigma}_{ns} (\delta u_s + z \delta \phi_s - c_1 z^3 \delta \varphi_{ns}) + \hat{\sigma}_{nz} \delta w_0] dz d\Gamma \\ &= - \int_{\Gamma} (\hat{N}_{nm} \delta u_n + \hat{M}_{nm} \delta \phi_n - c_1 \hat{P}_{nm} \delta \varphi_n + \hat{N}_{ns} \delta u_s + \hat{M}_{ns} \delta \phi_s - c_1 \hat{P}_{ns} \delta \varphi_{ns} + \hat{Q}_n \delta w_0) d\Gamma \\ \delta K &= \int_{\Omega_0} \int_{-\frac{h}{2}}^{\frac{h}{2}} \rho_0 [(\dot{u}_0 + z \dot{\phi}_x - c_1 z^3 \dot{\phi}_x)(\delta \dot{u}_0 + z \delta \dot{\phi}_x - c_1 z^3 \delta \dot{\phi}_x) \\ &\quad + (\dot{v}_0 + z \dot{\phi}_{\theta} - c_1 z^3 \dot{\phi}_{\theta})(\delta \dot{v}_0 + z \delta \dot{\phi}_{\theta} - c_1 z^3 \delta \dot{\phi}_{\theta}) + \dot{w}_0 \delta \dot{w}_0] dv \\ &= \int_{\Omega_0} [(I_0 \dot{u}_0 + I_1 \dot{\phi}_x - c_1 I_2 \dot{\phi}_x) \delta \dot{u}_0 + (I_1 \dot{u}_0 + I_2 \dot{\phi}_x - c_1 I_4 \dot{\phi}_x) \delta \dot{\phi}_x \\ &\quad - c_1 (I_3 \dot{u}_0 + I_4 \dot{\phi}_x - c_1 I_6 \dot{\phi}_x) \delta \dot{\phi}_x + (I_0 \dot{v}_0 + I_1 \dot{\phi}_{\theta} - c_1 I_3 \dot{\phi}_{\theta}) \delta \dot{v}_0 \\ &\quad + (I_1 \dot{v}_0 + I_2 \dot{\phi}_{\theta} - c_1 I_4 \dot{\phi}_{\theta}) \delta \dot{\phi}_{\theta} - c_1 (I_3 \dot{v}_0 + I_4 \dot{\phi}_{\theta} - c_1 I_6 \dot{\phi}_{\theta}) \delta \dot{\phi}_{\theta}] dx d\theta \end{aligned} \quad ()$$

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$$\begin{aligned} \begin{Bmatrix} N_{\alpha\beta} \\ M_{\alpha\beta} \\ P_{\alpha\beta} \end{Bmatrix} &= \int_{-\frac{h}{2}}^{\frac{h}{2}} \sigma_{\alpha\beta} \begin{Bmatrix} 1 \\ z \\ z^3 \end{Bmatrix} dz, & \begin{Bmatrix} Q_{\alpha} \\ R_{\alpha} \end{Bmatrix} &= \int_{-\frac{h}{2}}^{\frac{h}{2}} \sigma_{\alpha z} \begin{Bmatrix} 1 \\ z^2 \end{Bmatrix} dz \\ \begin{Bmatrix} \hat{N}_{\alpha\beta} \\ \hat{M}_{\alpha\beta} \\ \hat{P}_{\alpha\beta} \end{Bmatrix} &= \int_{-\frac{h}{2}}^{\frac{h}{2}} \hat{\sigma}_{\alpha\beta} \begin{Bmatrix} 1 \\ z \\ z^3 \end{Bmatrix} dz, & \begin{Bmatrix} \hat{Q}_{\alpha} \\ \hat{R}_{\alpha} \end{Bmatrix} &= \int_{-\frac{h}{2}}^{\frac{h}{2}} \hat{\sigma}_{\alpha z} \begin{Bmatrix} 1 \\ z^2 \end{Bmatrix} dz \end{aligned}$$

$$I_i = \int_{-\frac{h}{2}}^{\frac{h}{2}} \rho_0(z)^i dz \quad (i = 0, 1, 2, \dots, 6), \quad c_1 = \frac{4}{3h^2}, \quad c_2 = 3c_1 \quad ()$$

$$\varphi_{\alpha} = \phi_{\alpha} + \frac{\partial w_0}{\partial \alpha}, \quad (\alpha = x, y), \quad \varphi_{n\alpha} = \phi_{\alpha} + \frac{\partial w_0}{\partial \alpha}, \quad (\alpha = n, s)$$

$$\begin{aligned} & \dots \\ & \left(\right) \quad \left(\right) \quad \delta U, \delta K, \delta V \\ & \delta u_0, \delta v_0, \delta w_0, \delta \phi_x, \delta \phi_\theta \end{aligned}$$

$$\begin{aligned} & \frac{\partial N_{xx}}{\partial x} + \frac{1}{R} \frac{\partial N_{x\theta}}{\partial \theta} = I_0 \ddot{u}_0 + J_1 \ddot{\phi}_x - c_1 I_3 \frac{\partial \ddot{w}_0}{\partial x} \\ & \frac{\partial N_{x\theta}}{\partial r} + \frac{1}{R} \frac{\partial N_{\theta\theta}}{\partial \theta} + \frac{\bar{Q}_\theta}{R} + \frac{c_1}{R} \left(\frac{\partial P_{x\theta}}{\partial r} + \frac{1}{R} \frac{\partial P_{\theta\theta}}{\partial \theta} \right) = I_0 \ddot{v}_0 + J_1 \ddot{\phi}_\theta - c_1 I_3 \frac{1}{R} \frac{\partial \ddot{w}_0}{\partial \theta} \\ & \frac{\partial \bar{M}_{x\theta}}{\partial x} + \frac{1}{R} \frac{\partial \bar{M}_{\theta\theta}}{\partial \theta} - \bar{Q}_\theta = J_1 \ddot{v}_0 + K_2 \ddot{\phi}_\theta - c_1 J_4 \frac{1}{R} \frac{\partial \ddot{w}_0}{\partial \theta} \\ & \frac{\partial \bar{Q}_x}{\partial x} + \frac{1}{R} \frac{\partial \bar{Q}_\theta}{\partial \theta} + \frac{\partial}{\partial x} \left(N_{xx} \frac{\partial w_0}{\partial x} + N_{x\theta} \frac{1}{R} \frac{\partial w_0}{\partial \theta} \right) + \frac{1}{R} \frac{\partial}{\partial \theta} \left(N_{x\theta} \frac{\partial w_0}{\partial x} + N_{\theta\theta} \frac{1}{R} \frac{\partial w_0}{\partial \theta} \right) \\ & + c_2 \left(\frac{\partial^2 P_{xx}}{\partial x^2} + \frac{1}{R^2} \frac{\partial^2 P_{\theta\theta}}{\partial \theta^2} + 2 \frac{1}{R} \frac{\partial^2 P_{x\theta}}{\partial x \partial \theta} \right) - \frac{N_{\theta\theta}}{R} \\ & = I_0 \ddot{w}_0 - c_1^2 I_6 \left(\frac{\partial^2 w_0}{\partial x^2} + \frac{1}{R^2} \frac{\partial^2 \ddot{w}_0}{\partial \theta^2} \right) + c_1 \left[I_3 \left(\frac{\partial \ddot{u}_0}{\partial x} + \frac{1}{R} \frac{\partial \ddot{v}_0}{\partial \theta} \right) + J_4 \left(\frac{\partial \ddot{\phi}_x}{\partial x} + \frac{1}{R} \frac{\partial \ddot{\phi}_\theta}{\partial \theta} \right) \right] \\ & \frac{\partial \bar{M}_{xx}}{\partial x} + \frac{1}{R} \frac{\partial \bar{M}_{x\theta}}{\partial \theta} - \bar{Q}_r = J_1 \ddot{u}_0 + K_2 \ddot{\phi}_x - c_1 J_4 \frac{\partial \ddot{w}_0}{\partial x} \end{aligned} \quad ()$$

$$\begin{aligned} \begin{Bmatrix} \{N\} \\ \{M\} \\ \{P\} \end{Bmatrix} &= \begin{bmatrix} [A] & [B] & [E] \\ [B] & [D] & [F] \\ [E] & [F] & [H] \end{bmatrix} \begin{Bmatrix} \{\varepsilon^{(0)}\} \\ \{\varepsilon^{(1)}\} \\ \{\varepsilon^{(3)}\} \end{Bmatrix} - \begin{Bmatrix} \{N^T\} \\ \{M^T\} \\ \{P^T\} \end{Bmatrix} \quad \begin{Bmatrix} \{Q\} \\ \{R\} \end{Bmatrix} = \begin{bmatrix} [A] & [D] \\ [D] & [F] \end{bmatrix} \begin{Bmatrix} \gamma^{(0)} \\ \gamma^{(2)} \end{Bmatrix} \end{aligned} \quad ()$$

$$\begin{aligned} J_i &= I_i - c_1 I_{i+2}, \quad K_2 = I_2 - 2c_1 I_4 + c_1^2 I_6 \\ \bar{M}_{\alpha\beta} &= M_{\alpha\beta} - c_1 P_{\alpha\beta} \quad (\alpha, \beta = 1, 2, 6); \quad \bar{Q}_\alpha = Q_\alpha - c_2 R_\alpha \quad (\alpha = 4, 5) \end{aligned}$$

$$\begin{aligned} (N_{ij}^T, M_{ij}^T, P_{ij}^T) &= \int_{-h}^h \bar{Q}_{ij} \{\alpha\} \Delta T(z) (1, z, z^2) dz \\ (A_{ij}, B_{ij}, D_{ij}, E_{ij}, F_{ij}, H_{ij}) &= \int_{-h}^h \bar{Q}_{ij} (1, z, z^2, z^3, z^4, z^6) dz \\ Q_{11} = Q_{22} &= \frac{E(z)}{1-\nu(z)^2}, \quad Q_{12} = \frac{\nu(z)E(z)}{1-\nu(z)^2}, \quad Q_{44} = Q_{55} = Q_{66} = \frac{E(z)}{2(1+\nu(z))} \end{aligned} \quad ()$$

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$$-\frac{d}{dz} \left(k(z) \frac{dT}{dz} \right) = 0 \quad T\left(-\frac{h}{2}\right) = T_{in}, T\left(\frac{h}{2}\right) = T_{out} \quad ()$$

() $K(z)$

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$$T(z) = T_{out} + (T_{in} - T_{out})\eta(z)$$

$$\eta(z) = \frac{1}{C} \left[\left(\frac{2z+h}{2h} \right) - \frac{K_{out} - K_{in}}{(n+1)K_{out}} \left(\frac{2z+h}{2h} \right)^{n+1} + \frac{(K_{out} - K_{in})^2}{(2n+1)K_{out}^2} \left(\frac{2z+h}{2h} \right)^{2n+1} \right.$$

$$\left. - \frac{(K_{out} - K_{in})^3}{(3n+1)K_{out}^3} \left(\frac{2z+h}{2h} \right)^{3n+1} + \frac{(K_{out} - K_{in})^4}{(4n+1)K_{out}^4} \left(\frac{2z+h}{2h} \right)^{4n+1} - \frac{(K_{out} - K_{in})^5}{(5n+1)K_{out}^5} \left(\frac{2z+h}{2h} \right)^{5n+1} \right]$$

$$C = 1 - \frac{(K_{out} - K_{in})}{(n+1)K_{out}} + \frac{(K_{out} - K_{in})^2}{(2n+1)K_{out}^2} - \frac{(K_{out} - K_{in})^3}{(3n+1)K_{out}^3} + \frac{(K_{out} - K_{in})^4}{(4n+1)K_{out}^4} - \frac{(K_{out} - K_{in})^5}{(5n+1)K_{out}^5} \quad ()$$

() $T(z)$

$$u_0(x, \theta, t) \approx \sum_{j=1}^m u_j^e(t) \phi_j^e(x, \theta) \quad , \quad v_0(x, \theta, t) \approx \sum_{j=1}^m v_j^e(t) \phi_j^e(x, \theta) \quad , \quad w_0(x, \theta, t) \approx \sum_{j=1}^m w_j^e(t) \phi_j^e(x, \theta)$$

$$\phi_x(x, \theta, t) \approx \sum_{j=1}^m \phi_{xj}^e(t) \phi_j^e(x, \theta) \quad , \quad \phi_\theta(x, \theta, t) \approx \sum_{j=1}^m \phi_{\theta j}^e(t) \phi_j^e(x, \theta) \quad ()$$

$$\begin{Bmatrix} \phi_1^e \\ \phi_2^e \\ \phi_3^e \\ \phi_4^e \\ \phi_5^e \\ \phi_6^e \\ \phi_7^e \\ \phi_8^e \\ \phi_9^e \end{Bmatrix} = \frac{1}{4} \begin{Bmatrix} (1-\zeta)(1-\eta)(-\zeta-\eta-1) + (1-\zeta^2)(1-\eta^2) \\ (1+\zeta)(1-\eta)(\zeta-\eta-1) + (1-\zeta^2)(1-\eta^2) \\ (1+\zeta)(1+\eta)(\zeta+\eta-1) + (1-\zeta^2)(1-\eta^2) \\ (1-\zeta)(1+\eta)(-\zeta+\eta-1) + (1-\zeta^2)(1-\eta^2) \\ 2(1-\zeta^2)(1-\eta) - (1-\zeta^2)(1-\eta^2) \\ 2(1+\zeta)(1-\eta^2) - (1-\zeta^2)(1-\eta^2) \\ 2(1-\zeta^2)(1+\eta) - (1-\zeta^2)(1-\eta^2) \\ 2(1-\zeta)(1-\eta^2) - (1-\zeta^2)(1-\eta^2) \\ 4(1-\zeta^2)(1-\eta^2) \end{Bmatrix} \quad ()$$

ζ, η

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$$\begin{bmatrix} [M^{11}] & [0] & [M^{13}] & [M^{14}] & [0] \\ [0] & [M^{22}] & [M^{23}] & [0] & [M^{25}] \\ [M^{13}]^T & [M^{23}]^T & [M^{33}] & [M^{34}] & [M^{35}] \\ [M^{41}]^T & [0] & [M^{34}]^T & [M^{44}] & [0] \\ [0] & [M^{25}]^T & [M^{35}]^T & [0] & [M^{55}] \end{bmatrix} \begin{Bmatrix} \{\ddot{u}^e\} \\ \{\ddot{v}^e\} \\ \{\ddot{w}^e\} \\ \{\ddot{\phi}_r^e\} \\ \{\ddot{\phi}_\theta^e\} \end{Bmatrix} + \begin{bmatrix} [K^{11}] & [K^{12}] & [K^{13}] & [K^{14}] & [K^{15}] \\ [K^{21}] & [K^{22}] & [K^{23}] & [K^{24}] & [K^{25}] \\ [K^{31}] & [K^{32}] & [K^{33}] & [K^{34}] & [K^{35}] \\ [K^{41}] & [K^{42}] & [K^{43}] & [K^{44}] & [K^{45}] \\ [K^{51}] & [K^{52}] & [K^{53}] & [K^{54}] & [K^{55}] \end{bmatrix} \begin{Bmatrix} \{u^e\} \\ \{v^e\} \\ \{w^e\} \\ \{\phi_r^e\} \\ \{\phi_\theta^e\} \end{Bmatrix} = \begin{Bmatrix} \{F^1\} \\ \{F^2\} \\ \{F^3\} \\ \{F^4\} \\ \{F^5\} \end{Bmatrix} \quad ()$$

$$[M]\{\ddot{\delta}\} + [K]\{\delta\} + \{F\} = 0 \quad ()$$

$\{F\}, [M], [K] \qquad \qquad \qquad \{\delta\}, \{\ddot{\delta}\}$

von-Karman

Newmark

$$\begin{aligned}
 \{\delta\}_{i+1} &= \{\delta\}_i + \Delta t \cdot \{\dot{\delta}\}_i + 0.5(\Delta t)^2[(1-\beta)\{\ddot{\delta}\}_i + \beta\{\ddot{\delta}\}_{i+1}] \\
 \{\dot{\delta}\}_{i+1} &= \{\dot{\delta}\}_i + (\Delta t)[(1-\alpha)\{\ddot{\delta}\}_i + \alpha\{\ddot{\delta}\}_{i+1}]
 \end{aligned} \quad ()$$

$(i = 0)$

$$\{\ddot{\delta}\}_{i+1} = [M]^{-1}(\{F\} - [K]\{\delta\}_i) \quad ()$$

α, β

$$\alpha = \beta = 0.5$$

Runge-Kutta

T

$$\Delta t \leq \frac{T}{10}$$

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Δt

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FGM

- FGM

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$$R/h = 400, \frac{L^2}{Rh} = 300, T_0 = 300[K]$$

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[K]

T_0

[]

[]

[]

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$Si_3N_4 / SUS304$

n

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$ZrO_2 / Ti-6Al-4V$

-

$E.\alpha.\Delta T$

snap

through

$Si_3N_4 / SUS304$

)

$E.\alpha$

.(

$ZrO_2 / Ti-6Al-4V$

$Si_3N_4 / SUS304$

W_0

\bar{W}

()

n

FGM

$h = 1[mm]$

$\frac{L^2}{R.h} = 500$

/

$Si_3N_4 / SUS304$

n

$(T_i = T_0 = 300[K])$

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$Si_3N_4 / SUS304$

n

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$Si_3N_4 / SUS304$

n

($R/h = 30$)

$$E \cdot \alpha \cdot \Delta T$$

n

 $Si_3N_4 / SUS304$

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: A
: B
: c_1, c_2
: C
: C_v
: D
: E
: F
: h
: H
: i, j
: I, J
: K
: L
: M
: MP
: n
: N
: P
: Q
: R
: t
: T
: T_0
: u
: u_0
: U
: v
: v_0
: V
: w
: W_0

...

: \hat{w}

: \overline{W}

: x

: z

Newmark

: α

Newmark

: β

: δ

: $\delta, \dot{\delta}, \ddot{\delta}$

: $\varepsilon, \varepsilon^i$

: η

: θ

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: ξ

: ρ

: φ^e

: ψ

: ()

$$K_{ij}^{1\alpha} = \int_{\Omega^e} \left(\frac{\partial \varphi_i}{\partial x} N_{1j}^\alpha + \frac{\partial \varphi_i}{\partial y} N_{6j}^\alpha \right) dx dy \quad , \quad K_{ij}^{2\alpha} = \int_{\Omega^e} \left(\frac{\partial \varphi_i}{\partial x} N_{6j}^\alpha + \frac{\partial \varphi_i}{\partial y} N_{2j}^\alpha + \varphi_i \frac{1}{R} \hat{Q}_{2j}^\alpha + \frac{c_1}{R} \left(\frac{\partial \varphi_i}{\partial x} P_{6j}^\alpha + \frac{\partial \varphi_i}{\partial y} P_{2j}^\alpha \right) \right) dx dy$$

$$K_{ij}^{3\alpha} = \int_{\Omega^e} \left[\frac{\partial \varphi_i}{\partial x} \hat{Q}_{1j}^\alpha + \frac{\partial \varphi_i}{\partial y} \hat{Q}_{2j}^\alpha - c_1 \left(\frac{\partial^2 \varphi_i}{\partial x^2} P_{1j}^\alpha + 2 \frac{\partial^2 \varphi_i}{\partial x \partial y} P_{6j}^\alpha + \frac{\partial^2 \varphi_i}{\partial y^2} P_{2j}^\alpha \right) + \frac{\partial \varphi_i}{\partial x} \left(N_{1j}^\alpha \frac{\partial w_0}{\partial x} + N_{6j}^\alpha \frac{\partial w_0}{\partial y} \right) + \frac{\partial \varphi_i}{\partial y} \left(N_{6j}^\alpha \frac{\partial w_0}{\partial x} + N_{2j}^\alpha \frac{\partial w_0}{\partial y} \right) - \frac{\varphi_i}{R} N_{2j}^\alpha \right] dx dy$$

$$K_{ij}^{4\alpha} = \int_{\Omega^e} \left(\frac{\partial \varphi_i}{\partial x} \hat{M}_{1j}^\alpha + \frac{\partial \varphi_i}{\partial y} \hat{M}_{6j}^\alpha - \varphi_i \hat{Q}_{1j}^\alpha \right) dx dy \quad , \quad K_{ij}^{5\alpha} = \int_{\Omega^e} \left(\frac{\partial \varphi_i}{\partial x} \hat{M}_{6j}^\alpha + \frac{\partial \varphi_i}{\partial y} \hat{M}_{2j}^\alpha - \varphi_i \hat{Q}_{2j}^\alpha \right) dx dy$$

$\beta \qquad \qquad \alpha \qquad \qquad \qquad j \qquad \qquad i \qquad \qquad K_{ij}^{\alpha\beta}$

: $\frac{\partial}{\partial y} \equiv \frac{\partial}{R \partial \theta} \qquad i, j = 1, 2, \dots, N, \quad \alpha = 1, 2, \dots, 5 :$.

$$N_{1j}^1 = A_{11} \frac{\partial \varphi_j}{\partial x} + A_{16} \frac{\partial \varphi_j}{\partial y} \quad , \quad N_{1j}^2 = A_{12} \frac{\partial \varphi_j}{\partial y} + A_{16} \frac{\partial \varphi_j}{\partial x} + E_{12} \frac{c_2}{R} \frac{\partial \varphi_j}{\partial y} + E_{16} \frac{c_2}{R} \frac{\partial \varphi_j}{\partial x}$$

$$N_{1j}^3 = A_{11} \left(\frac{1}{2} \frac{\partial w_0}{\partial x} \frac{\partial \varphi_j}{\partial x} + A_{12} \frac{1}{2} \frac{\partial w_0}{\partial y} \frac{\partial \varphi_j}{\partial y} + A_{16} \frac{\partial w_0}{\partial x} \frac{\partial \varphi_j}{\partial y} - c_2 (E_{11} \frac{\partial^2 \varphi_j}{\partial x^2} + E_{12} \frac{\partial^2 \varphi_j}{\partial y^2} + E_{16} 2 \frac{\partial \varphi_j}{\partial x} \frac{\partial \varphi_j}{\partial y}) \right)$$

$$N_{1j}^4 = B_{11} \frac{\partial \varphi_j}{\partial x} + B_{16} \frac{\partial \varphi_j}{\partial y} - c_2 (E_{11} \frac{\partial \varphi_j}{\partial x} + E_{16} \frac{\partial \varphi_j}{\partial y}) \quad , \quad N_{1j}^5 = B_{12} \frac{\partial \varphi_j}{\partial y} + B_{16} \frac{\partial \varphi_j}{\partial x} - c_2 (E_{11} \frac{\partial \varphi_j}{\partial y} + E_{16} \frac{\partial \varphi_j}{\partial x})$$

$$N_{2j}^1 = A_{12} \frac{\partial \varphi_j}{\partial x} + A_{26} \frac{\partial \varphi_j}{\partial y} \quad , \quad N_{2j}^2 = A_{22} \frac{\partial \varphi_j}{\partial y} + A_{26} \frac{\partial \varphi_j}{\partial x} + \frac{c_2}{R} (E_{22} \frac{\partial \varphi_j}{\partial y} + E_{26} \frac{\partial \varphi_j}{\partial x})$$

$$N_{2j}^3 = A_{12} \frac{1}{2} \frac{\partial w_0}{\partial x} \frac{\partial \varphi_j}{\partial x} + A_{22} \frac{1}{2} \frac{\partial w_0}{\partial y} \frac{\partial \varphi_j}{\partial y} + A_{26} \frac{\partial w_0}{\partial x} \frac{\partial \varphi_j}{\partial y} - c_2 (E_{12} \frac{\partial^2 \varphi_j}{\partial x^2} + E_{22} \frac{\partial^2 \varphi_j}{\partial y^2} + E_{26} \frac{\partial^2 \varphi_j}{\partial x \partial y})$$

$$N_{2j}^4 = B_{12} \frac{\partial \varphi_j}{\partial x} + B_{26} \frac{\partial \varphi_j}{\partial y} - c_2 (E_{12} \frac{\partial \varphi_j}{\partial x} + E_{26} \frac{\partial \varphi_j}{\partial y}) \quad , \quad N_{2j}^5 = B_{22} \frac{\partial \varphi_j}{\partial y} + B_{26} \frac{\partial \varphi_j}{\partial x} - c_2 (E_{22} \frac{\partial \varphi_j}{\partial y} + E_{26} \frac{\partial \varphi_j}{\partial x})$$

$$N_{6j}^1 = A_{16} \frac{\partial \varphi_j}{\partial x} + A_{66} \frac{\partial \varphi_j}{\partial y} \quad , \quad N_{6j}^2 = A_{26} \frac{\partial \varphi_j}{\partial y} + A_{66} \frac{\partial \varphi_j}{\partial x} + \frac{c_2}{R} (E_{26} \frac{\partial \varphi_j}{\partial y} + E_{66} \frac{\partial \varphi_j}{\partial x})$$

$$N_{6j}^3 = A_{16} \frac{1}{2} \frac{\partial w_0}{\partial x} \frac{\partial \varphi_j}{\partial x} + A_{26} \frac{1}{2} \frac{\partial w_0}{\partial y} \frac{\partial \varphi_j}{\partial y} + A_{16} \frac{\partial w_0}{\partial x} \frac{\partial \varphi_j}{\partial y} - c_2 (E_{16} \frac{\partial^2 \varphi_j}{\partial x^2} + E_{26} \frac{\partial^2 \varphi_j}{\partial y^2} + E_{66} \frac{\partial^2 \varphi_j}{\partial y \partial x})$$

$$N_{6j}^4 = B_{16} \frac{\partial \varphi_j}{\partial x} + B_{66} \frac{\partial \varphi_j}{\partial y} - c_2 (E_{16} \frac{\partial \varphi_j}{\partial x} + E_{66} \frac{\partial \varphi_j}{\partial y}) \quad , \quad N_{6j}^5 = B_{26} \frac{\partial \varphi_j}{\partial y} + B_{66} \frac{\partial \varphi_j}{\partial x} - c_2 (E_{16} \frac{\partial \varphi_j}{\partial y} + E_{66} \frac{\partial \varphi_j}{\partial x})$$

:

$$\begin{aligned}
P_{6j}^3 &= E_{16} \frac{1}{2} \frac{\partial w_0}{\partial x} \frac{\partial \varphi_j}{\partial x} + E_{26} \frac{1}{2} \frac{\partial w_0}{\partial y} \frac{\partial \varphi_j}{\partial y} + E_{66} \frac{\partial w_0}{\partial x} \frac{\partial \varphi_j}{\partial y} - c_2 (H_{16} \frac{\partial^2 \varphi_j}{\partial x^2} + H_{26} \frac{\partial^2 \varphi_j}{\partial y^2} + H_{66} \frac{\partial^2 \varphi_j}{\partial x \partial y}) \\
P_{2j}^3 &= E_{12} \frac{1}{2} \frac{\partial w_0}{\partial x} \frac{\partial \varphi_j}{\partial x} + E_{22} \frac{1}{2} \frac{\partial w_0}{\partial y} \frac{\partial \varphi_j}{\partial y} + E_{26} \frac{\partial w_0}{\partial x} \frac{\partial \varphi_j}{\partial y} - c_2 (H_{12} \frac{\partial^2 \varphi_j}{\partial x^2} + H_{22} \frac{\partial^2 \varphi_j}{\partial y^2} + H_{26} \frac{\partial^2 \varphi_j}{\partial x \partial y}) \\
P_{2j}^4 &= F_{12} \frac{\partial \varphi_j}{\partial x} + F_{26} \frac{\partial \varphi_j}{\partial y} - c_2 (H_{12} \frac{\partial \varphi_j}{\partial x} + H_{26} \frac{\partial \varphi_j}{\partial y}) \quad , \quad P_{2j}^5 = F_{22} \frac{\partial \varphi_j}{\partial y} + F_{26} \frac{\partial \varphi_j}{\partial x} - c_2 (H_{22} \frac{\partial \varphi_j}{\partial y} + H_{26} \frac{\partial \varphi_j}{\partial x}) \\
Q_{1j}^1 &= 0 \quad , \quad Q_{1j}^2 = A_{44} \frac{-1}{R} \varphi_j + D_{44} \frac{c_1}{R} \varphi_j - c_2 (D_{44} \frac{-1}{R} \varphi_j + F_{44} \frac{c_1}{R} \varphi_j) \\
Q_{1j}^3 &= A_{44} \frac{\partial \varphi_j}{\partial y} + A_{45} \frac{\partial \varphi_j}{\partial x} + D_{44} (-c_1 \frac{\partial \varphi_j}{\partial y}) + D_{45} (-c_1 \frac{\partial \varphi_j}{\partial x}) - c_2 (D_{44} \frac{\partial \varphi_j}{\partial y} + D_{45} \frac{\partial \varphi_j}{\partial x} + F_{44} (-c_1 \frac{\partial \varphi_j}{\partial y}) + F_{45} (-c_1 \frac{\partial \varphi_j}{\partial x})) \\
Q_{1j}^4 &= A_{45} \varphi_j - D_{45} c_1 \varphi_j - c_2 (D_{45} \varphi_j - F_{45} c_1 \varphi_j) \quad , \quad Q_{1j}^5 = A_{44} \varphi_j - D_{44} c_1 \varphi_j - c_2 (D_{44} \varphi_j - F_{44} c_1 \varphi_j) \\
M_{ij}^{11} &= I_0 S_{ij}^0, \quad M_{ij}^{12} = 0, \quad M_{ij}^{13} = -c_1 I_3 S_{ij}^{0x}, \quad M_{ij}^{14} = J_1 S_{ij}^0, \quad M_{ij}^{22} = I_0 S_{ij}^0, \quad M_{ij}^{23} = -c_1 I_3 S_{ij}^{0y}, \quad M_{ij}^{24} = 0 \\
M_{ij}^{25} &= J_1 S_{ij}^0, \quad M_{ij}^{15} = 0, \quad M_{ij}^{33} = I_0 S_{ij}^1 + c_1^2 I_6 (S_{ij}^{xx} + S_{ij}^{yy}), \quad M_{ij}^{34} = -c_1 J_4 S_{ij}^{0y}, \quad M_{ij}^{35} = -c_1 J_4 S_{ij}^{0x} \\
M_{ij}^{44} &= K_2 S_{ij}^0, \quad M_{ij}^{45} = 0, \quad M_{ij}^{55} = K_2 S_{ij}^0, \quad S_{ij}^{0x} = \int_{\Omega^e} \varphi_i \varphi_j dx dy, \quad S_{ij}^{0x} = \int_{\Omega^e} \varphi_i \frac{\partial \varphi_j}{\partial x} dx dy \\
S_{ij}^{0y} &= \int_{\Omega^e} \varphi_i \frac{\partial \varphi_j}{\partial y} dx dy, \quad S_{ij}^1 = S_{ij}^0, \quad S_{ij}^{xx} = \int_{\Omega^e} \frac{\partial \varphi_i}{\partial x} \frac{\partial \varphi_j}{\partial x} dx dy, \quad S_{ij}^{yy} = \int_{\Omega^e} \frac{\partial \varphi_i}{\partial y} \frac{\partial \varphi_j}{\partial y} dx dy
\end{aligned}$$

FGM

| | $E[GPa]$ | ν | $\alpha[K^{-1}]$ | $\kappa [W / mK]$ | $\rho [kg / m^3]$ | $C_v [J / kgK]$ |
|-----------------|----------|-------|------------------|-------------------|-------------------|-----------------|
| Zirconia | / | / | / e- | / | | / |
| Silicon nitride | / | / | / e | / | | / |
| Ti-6Al-4V | / | / | / e- | | | / |
| Stainless steel | / | / | / e- | / | | / |

...

[K] FGM

| n | $Si_3N_4 / SUS304$ | | $SUS304 / Si_3N_4$ | | $ZrO_2 / Ti-6Al-4V$ | | $Ti-6Al-4V / ZrO_2$ | |
|---|--------------------|---|--------------------|---|---------------------|---|---------------------|---|
| | [] | | [] | | [] | | [] | |
| | / | / | / | / | / | / | / | / |
| / | / | / | / | / | / | / | / | / |
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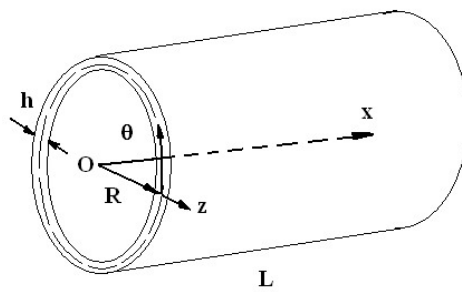
[kN] $Si_3N_4 / SUS304$

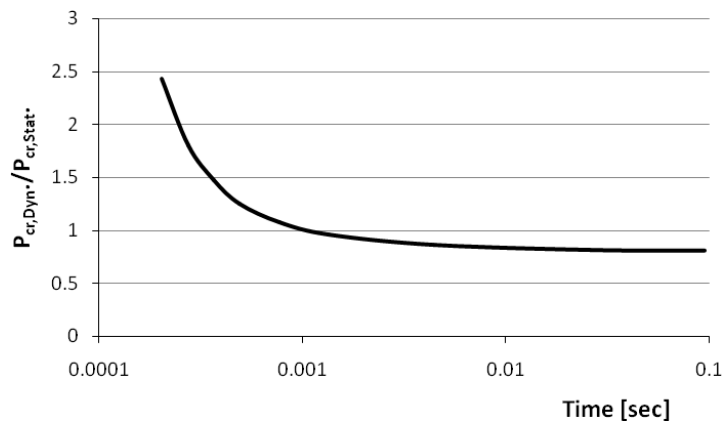
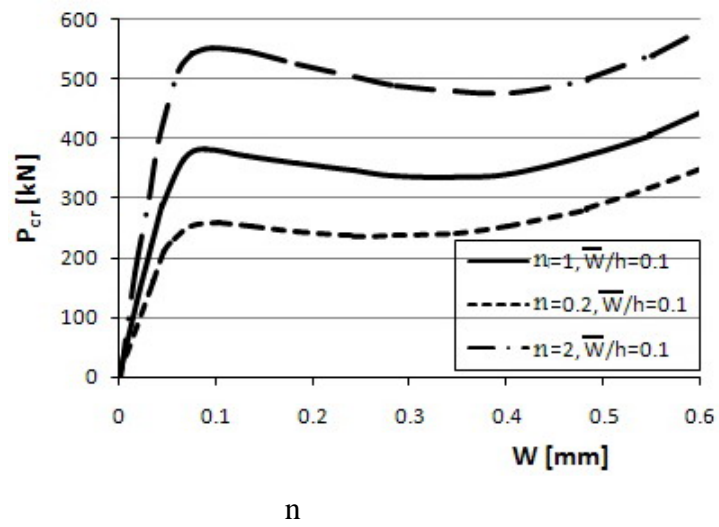
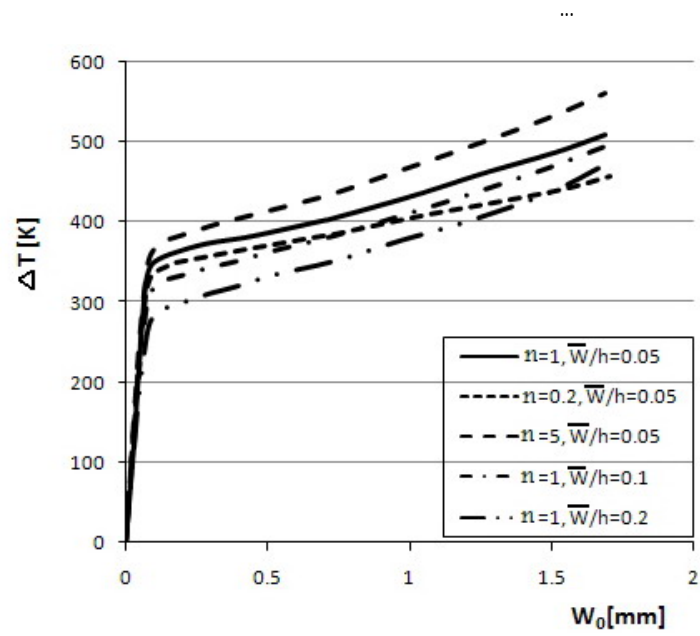
| $R/h = 300, T_i = T_0 = 300[K]$ | | | |
|---------------------------------|--------------------|--------------------|--------------------|
| n | $T_{out} = 300[K]$ | $T_{out} = 600[K]$ | $T_{out} = 900[K]$ |
| / | / | / | / |
| | / | / | / |
| | / | / | / |
| $R/h = 30, T_i = T_0 = 300[K]$ | | | |
| n | $T_{out} = 300[K]$ | $T_{out} = 600[K]$ | $T_{out} = 900[K]$ |
| / | / | / | / |
| | / | / | / |
| | / | / | / |

$Si_3N_4 / SUS304$

[kN]

| $R/h = 300, T_i = T_0 = 300[K]$ | | | | |
|---------------------------------|--------------------|---|--------------------|---|
| n | $T_{out} = 600[K]$ | | $T_{out} = 900[K]$ | |
| | / | / | / | / |
| | / | / | / | / |
| | / | / | / | / |
| $R/h = 30, T_i = T_0 = 300[K]$ | | | | |
| n | $T_{out} = 600[K]$ | | $T_{out} = 900[K]$ | |
| | / | / | / | / |
| | / | / | / | / |
| | / | / | / | / |





Abstract

In the present paper, dynamic buckling analysis of a circular cylindrical shell with initial geometric imperfections and a temperature distribution, under axial load is investigated using the third order shear deformation theory. A second order element is used, the resulted nonlinear equations are solved using an iterative numerical time integration method in conjunction with incremental loading and updating methods, and the buckling load is determined employing Budiansky's criterion. Since no work is developed in literature in dynamic buckling of FGM cylindrical shells field so far, present results are compared with results of the static buckling analyses performed by other references, as a first stage. Then, influences of various parameters on the dynamic buckling of the FGM shells are investigated. Obtained results indicate the effects of the power of the constitutive law equation and specially, temperature difference of the inner and outer surfaces on the buckling load. Furthermore, results reveal that the buckling load may exceed the static buckling load in special loading conditions.