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$$U = \sum_{t=0}^T \frac{V(C_t)}{(1+\rho)^t}$$

$$U = \sum_{t=0}^T \frac{V(C_t)}{(1+\rho)^t} \quad t=0, 1, \dots, T \quad ()$$

1. Subjective Factors.

T

P

V'

$$V'' < 0$$

$$t = 1 \quad t = 0$$

$$(C_1, C_2)$$

$$dC_t = 0 \quad t > 1$$

$$dU = V'(C_0) dC_0 + V'(C_1) dC_1 / (1 + \rho)$$

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$$dU = 0$$

$$(dC_1/dC_0)_{U=U} = - [V'(C_0)/V'(C_1)](1 + \rho)$$

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$$|dC_1/dC_0| > 1$$

$$C_1 > C_0$$

$$\rho = 0$$

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$$\rho > 0$$

$$C_1 = C_0$$

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$$V'' < 0$$

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1. Time Preference.

2. Diminishing Marginal Utility(DMU).

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B C_0^A A B A
 $t=0$
 $t=1$ C_0^B

$$C_0^A = C_1^A$$

$$C_0^B = C_1^B$$

A

B

A

B

A		B			
	$t = 0$	$t = 1$		$t = 0$	$t = 1$
	U'_{01}	U'_{11}		V'_{01}	V'_{11}
	U'_{02}	U'_{12}		V'_{02}	V'_{12}
.			.		
.			.		
.			.		
i	U'_{0i}	U'_{1i}	j	V'_{0j}	V'_{1j}
T	U'_{0T}	U'_{1T}	H	V'_{0H}	V'_{1H}

$$\begin{array}{l}
 U'_{0i} = U'_i \quad i = 1, \dots, T \quad \text{A} \\
 U'_{1i} \\
 V'_{0j} = V'_{1j} = V'_j \quad j = 1, \dots, H \quad \text{B} \\
 \text{B} \quad \text{n} \quad \text{A} \\
 \text{n} (t = 0)
 \end{array}$$

$$\begin{array}{l}
 U'_{T+1}, U'_{T+2}, \dots, U'_{T+n} \\
 : \\
 \Sigma U'_{T+q} \quad \text{A} \\
 q = 1, \dots, n
 \end{array}$$

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_____ (t=1)

m

(t=1)

: t = 1

$$\Sigma U'_{T-r} \quad r = 0, \dots, m-1 \quad A$$

$$i = (m-n)/n$$

$$\text{if } m = n \longrightarrow i = 0$$

$$\text{if } m > n \longrightarrow i > 0$$

$$\text{if } m < n \longrightarrow i < 0$$

$$\text{if } m = n \longrightarrow \Sigma U'_{T+q} < |\Sigma U'_{T-r}| \quad ()$$

A

$$\Sigma U'_{T+q} = |\Sigma U'_{T-r}| \quad ()$$

A

t=0

B

B

m < n

n

$$V'_H, V'_{H-1}, \dots, V'_{H(n-1)}$$

: A

$$\Sigma V'_{H-y} \quad y = 0, \dots, n-1$$

m

:

$$\Sigma V'_{H+z} \quad z = 1, \dots, m$$

B

$$\Sigma V'_{H-y} = |\Sigma V'_{H+z}| \quad ()$$

n < m

B

$$\begin{array}{l}
 \rho < 1 & A \\
 \Sigma U'_{T+q} \quad q = 1, \dots, n & A \\
 (t = 1) & \\
 |\Sigma U'_{T-r}| / (1+\rho) \quad r = 0, \dots, m-1 & : \\
 \Sigma U'_{T+q} = |\Sigma U'_{T-r}| / (1+\rho) & () \\
 \quad \quad \quad m \quad \quad \quad \rho = 0 & \\
 B & \\
 \rho A > \rho B & : \\
 \\
 t = & A \quad \quad \quad \rho > 0 \\
 & \quad \quad \quad n \quad 0 \\
 \\
 U'_{T+1}, U'_{T+2}, \dots, U'_{T+n} & \\
 : & \\
 U'_{T+1} = U'_{T+2} = \dots = U'_{T+n} & \\
 \quad \quad \quad t=0 & \\
 \\
 \Sigma U'_{T+q} = nU' \quad q = 1, \dots, n & () \\
 \end{array}$$

$$|\Sigma U'_{T+n-r}|/(1+\rho) = \Sigma U'_{T+q} \quad ()$$

$$|\Sigma U'_{T+n-r}| > \Sigma U'_{T+q} \quad ()$$

n

m

A

A

A

t=1

»:

t=0 A «

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$U'/(1+\rho)$

: $U' > U'/(1+\rho)$ $U'/(1+\rho)$ t=1

A

t=1

$$nU'(1+\rho) = mU'$$

$$n(1+\rho) = m$$

$$m > n \quad i > 0$$

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$$V = \sum_{j=0,1} D^j U(C_i^{t+j}) \quad , \quad \begin{matrix} j=0,1 \\ i=1,2 \end{matrix} \quad ()$$

D i t

P_t t

g

$$C_{1t} + \beta C_{2t+1} = P_t \quad ()$$

$$\beta = 1/(1+g)$$

$$D/\beta = U'_1/U'_2 \quad ()$$

D β

$$\text{If } \beta > D \longrightarrow U'_2 > U'_1 \longrightarrow C_{1t} > C_{2t+1} \quad ()$$

$$P_t C_{1t} = \alpha P_{t+1} C_{2t+1} \quad ()$$

(α)

$$P_{t+1}/P_t = (1/\alpha) C_{1t}/C_{2t+1} \quad ()'$$

$$\pi = (1/\alpha)(C_{1t}/C_{2t+1}) - 1 \quad ()''$$

D β ''

$$V = \ln C_{1t} + D \ln C_{2t+1} \quad ()$$

$$\beta / D = C_{1t} / C_{2t+1} \quad ()$$

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$$\pi = (1/\alpha)(\beta/D) - 1 \quad ()$$

) β

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$$\pi = (2/\alpha) - 1 \quad (D = /) \quad /$$

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