

\*

-

-

( // , // )

:

. [ - ]

PID

. [ - ]

Irrational

Irrational

Irrational

$$N(s) = (s^n + a_1 s^{n-1} + \dots + a_n) \quad (1)$$

$$-K(s^m + b_1 s^{m-1} + \dots + b_m) e^{-st_d} = 0 \quad (2)$$

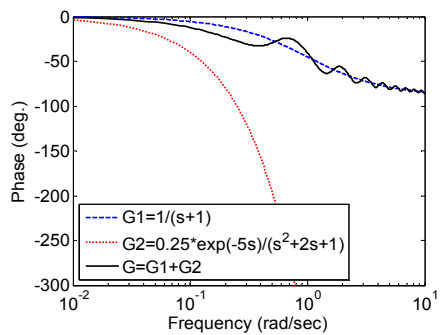
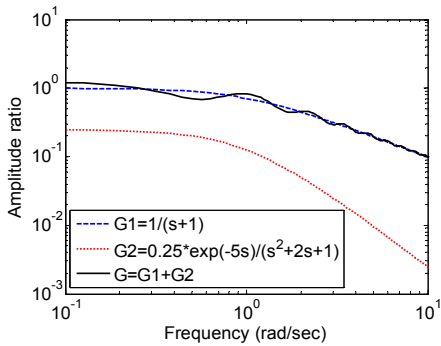
$$\frac{P_1(s)}{P_1(s)} = K \frac{P_2(s)}{P_2(s)} \quad (3)$$

$$m \quad n \quad K$$

LHP RHP

$$[ - ] \quad (4)$$

QRDS



$$[ - ] \quad (5)$$

LHP RHP

$$n \geq m, |K| \leq 1 \quad \text{Bode} \quad :$$

$$(6)$$

$$G_p(s) = \frac{P_1(s) - P_2(s) e^{-st_d}}{Q(s)} \quad (7)$$

$$Q(s) = P_2(s) - P_1(s) s$$

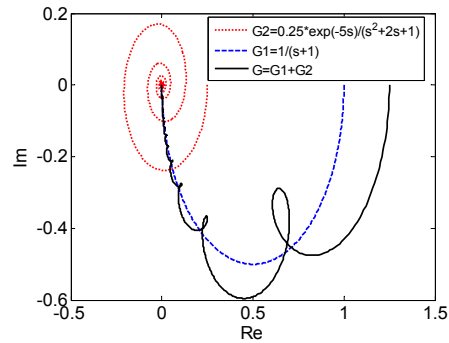
$$Q(s) \quad P_2(s) \quad P_1(s)$$

Nyquist Bode ( ) ( )  
 (n = -2, m = -1, K = 4)

$|K| < 1$   $n \geq m$  [ - - ]  
 ( )  
 (LHP)

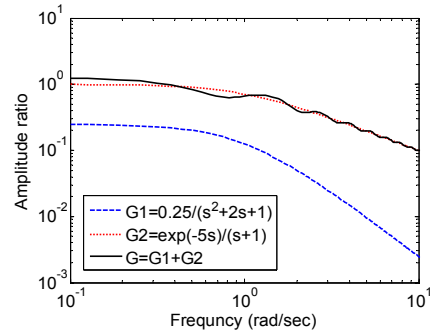
( ) ( )  
 (n = -1, m = -2, Nyquist Bode  
 K = 0.25)

$n < m$ ,  $|K| < 1$   $n > m$ ,  $|K| > 1$

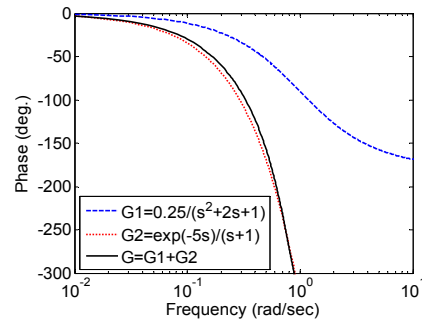


( ) [ - ]

$n \geq m$ ,  $|K| \leq 1$  Nyquist :



( )



[ - ] [ - ]

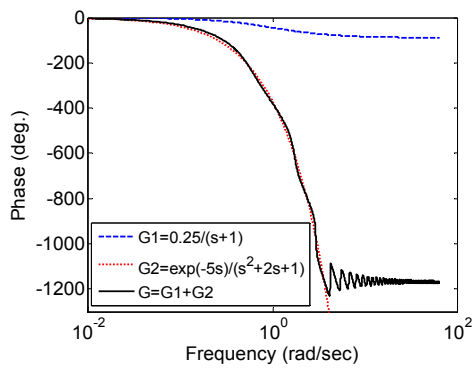
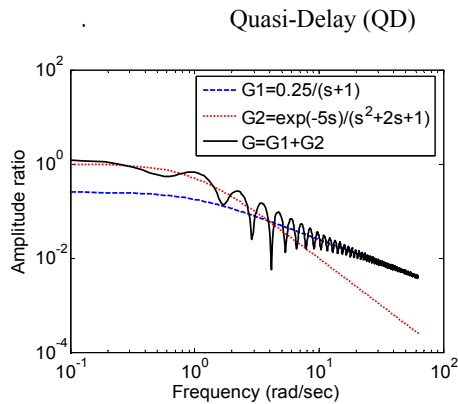
$n \leq m$ ,  $|K| > 1$  Bode :

Irrational

$$G(s) = G_1(s) + G_2(s) = \frac{P_1(s)}{Q_1(s)} + \frac{P_2(s)}{Q_2(s)} e^{-sT_d} = G_1(s) + G_2'(s) e^{-sT_d} \quad ( )$$

$|K| > 1$   $n \leq m$

)  $G_2(s)$   $G_1(s)$   
 G(s) (  $n \geq m$ ,  $|K| < 1$  or  $n > m$ ,  $|K| = 1$  )



$n > m, |K| > 1$       **Bode**      :

$n < m, |K| < 1$

$G_1(s)$

( )

$G_2(s)$

)

( )

Retarded-Delay-QRDS (RD)

Non-Delay-QRDS

Delay-QRDS    “Quasi-Delay-QRDS (QD) (ND)

Retarded-Delay-QRDS (RD) (D)

$G_1(s)$

$G(s)$

$G_1(s)$

$G_1(s)$

Non Delay-QRDS (ND)

( ) ( )

$G_2(s)$

(  $n \leq m, |K| > 1$  or  $n < m, |K| = 1$  )

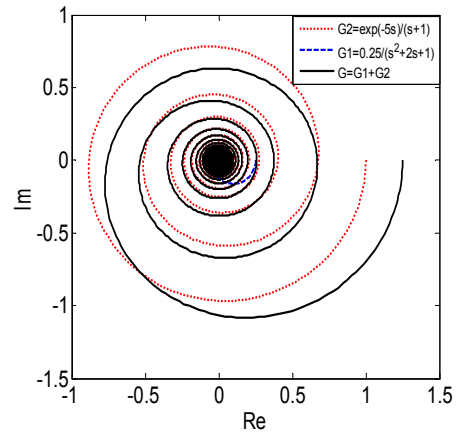
$G_2(s)$

$G(s)$

$G_2(s)$

( ) ( )

Delay-QRDS (D)



$n \leq m, |K| > 1$       **Nyquist**      :

“ ”

$n > m, |K| > 1$

(K

)

$G_2(s)$

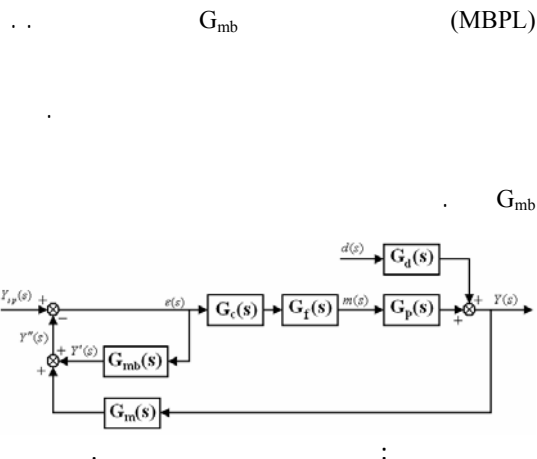
$G_1(s)$

$n > m$

( )

$$G_{mb} = G_p^- [1 - G_p^+(s)]$$

Model Bypass Phase Limiter



$$\frac{Y(s)}{Y_{sp}(s)} = \frac{G_c(s)G_f(s)G_p(s)}{1 + G_{mb}(s) + G_c(s)G_f(s)G_p(s)G_m(s)}$$

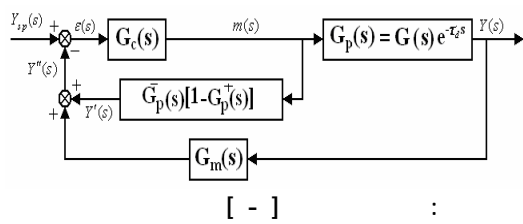
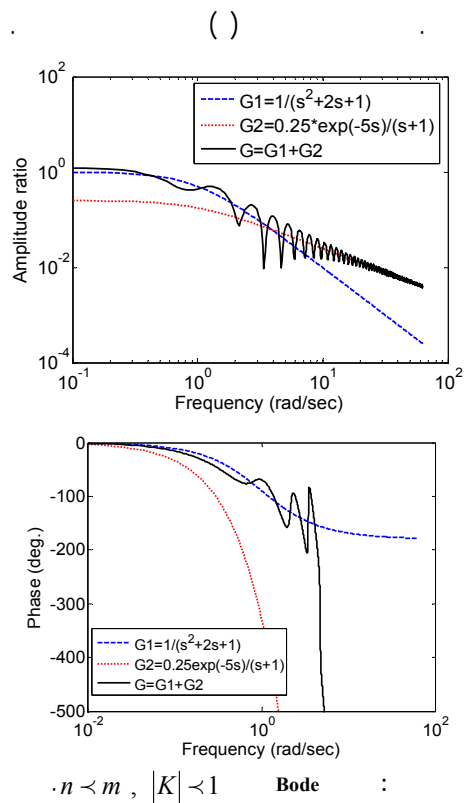
$$\frac{Y(s)}{d(s)} = \frac{G_d(s) + G_{mb}(s)G_d(s)}{1 + G_{mb}(s) + G_c(s)G_f(s)G_p(s)G_m(s)}$$

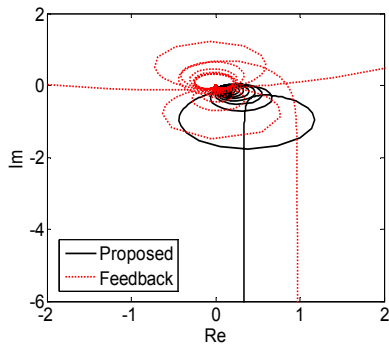
PI

$$K_m \quad 1/K_m$$

$$1 + G_{mb}(s) + G_c(s)G_f(s)G_p(s)G_m(s) = 0$$

Open loop =  $G_{mb}(s) + G_c(s)G_f(s)G_p(s)G_m(s)$





Nyquist :

$$\begin{pmatrix} \phantom{0} \\ \phantom{0} \end{pmatrix} G_{mb}$$

$$\begin{pmatrix} \phantom{0} \\ \phantom{0} \end{pmatrix}$$

$$\varepsilon(s) = \frac{Y_{sp}(s)}{1 + G_{mb}(s) + G_c(s)G_f(s)G_p(s)G_m(s)} \quad ( )$$

$$\varepsilon(s) = \frac{Y_{sp}(s)}{1 + G_c(s)G_f(s)G_p(s)G_m(s)} \quad ( )$$

:[ ]

$$G(s) = G_n(s) + \delta G(s) \quad ( )$$

$$\delta G(s) \quad G(s) \quad ( )$$

$$\delta G(s) .$$

G(s)

G<sub>mb</sub>

( )

: ( )

$$|\delta G(s)| = \frac{|1 + G_{mb}(s) + G_c(s)G_n(s)|}{|G_c(s)|} \quad ( )$$

$$|\delta G(s)| = \frac{|1 + G_c(s)G_n(s)|}{|G_c(s)|} \quad ( )$$

( ) ( )

( )

$$G_p(s) = 0.5/(s+1) + [6 \exp(-8s)/(s+1)]$$

$$G_{mb}(s) = 6/(s+1)$$

K<sub>mb</sub>

ISE

$G_1(s)$

$G_2(s)$

:

Non-Delay-QRDS (ND)

[ ]

PI

( )

:

$G_{mb}(s)$

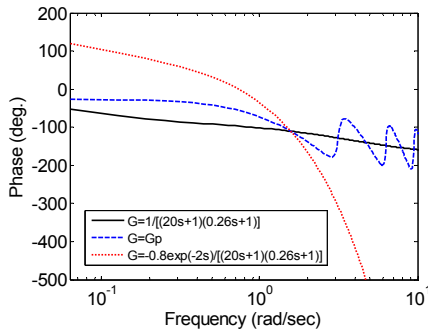
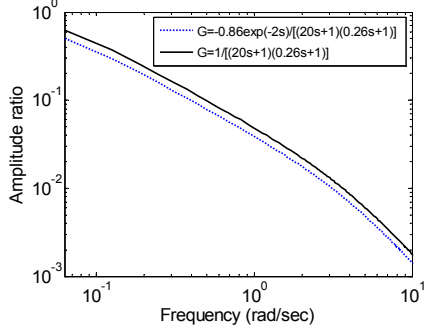
$$\frac{\overline{\delta T}(L, s)}{\overline{\delta T}_g(0, s)} = \frac{b(s)}{a(s)} (1 - e^{-\frac{a}{v_s} L}) \quad ( )$$

( )

[ ]

$$G_p(s) = G_1(s) + G_2'(s) e^{-sL_d}$$

$$G_p = \frac{T(s)}{T_g(s)} = \frac{1 - 0.8 \exp(-2s)}{(20s + 1)(0.26s + 1)} \quad ( )$$



(ND)

Bode

:

$G_{mb}(s)$

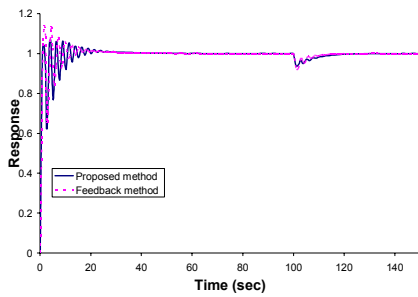
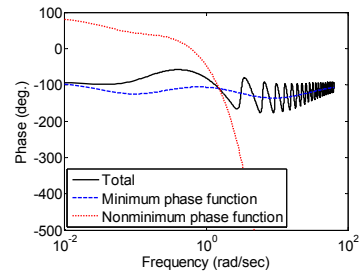
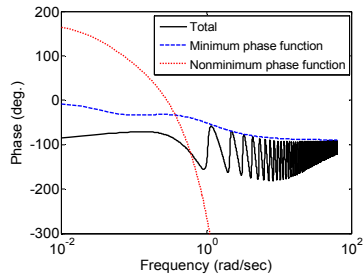
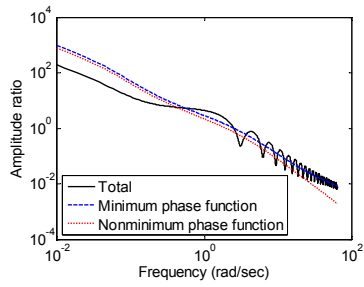
$G_{mb}(s)$

( ) Bode

$G_2$   $G_1$

$$-1 \leq t_d \leq -6$$

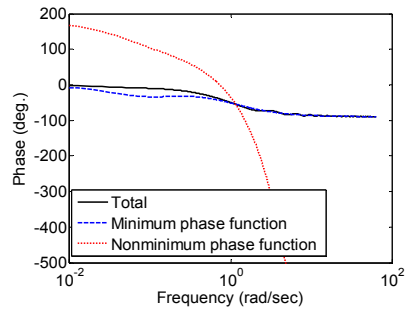
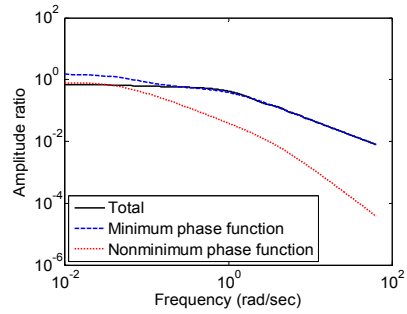
( )



(ND)

$$G_{mb}(s) = 0.5/(s+1)$$

( )



$G_{mb}(s)$

(ND)

ISE

$$G_c(s) = 55.2531 + \frac{9.7819}{s}$$

( )

$$G_c(s) = 33.436 + \frac{8.585}{s}$$



( )

( )

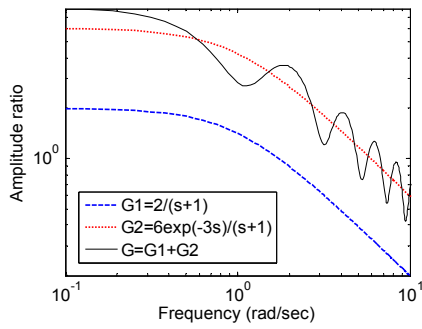
Delay-

QRDS (D)

( )

$$G_p(s) = \frac{2}{s+1} + \frac{6 \exp(-3s)}{s+1}$$

( )



( )

( )

			IAE
	/	/	/
	/	/	/

(D)

ISE

$$G_{mb}(s) = \frac{4}{s+1}$$

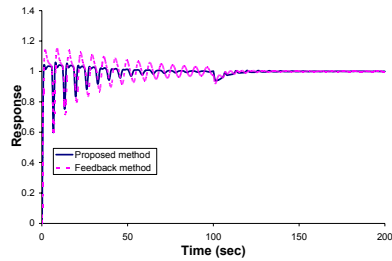
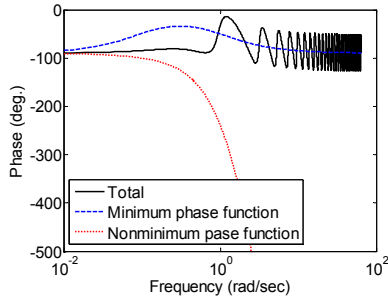
$$G_c(s) = 0.5123 + \frac{0.2346}{s}$$

$$G_c(s) = 0.1639 + \frac{0.0409}{s}$$

( )

+

( )

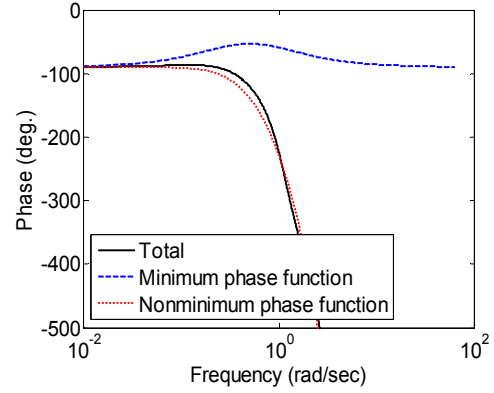


			IAE
	/	/	
	/		

/D-QRDS

( )

$G_{mb}(s)$



$G_{mb}(s)$

( )

(D)

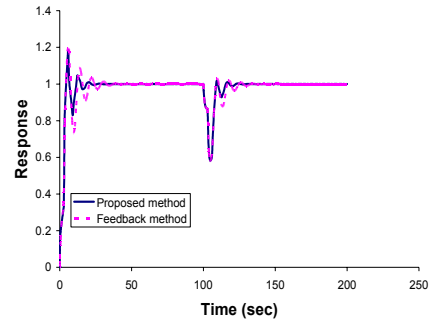
( )

$\Delta x$

( )

$$vA_i\rho C T - vA_i\rho C(T + \frac{\partial T}{\partial x}\Delta x) + \pi D_i h_i \Delta x (T_w - T) \quad (A-1)$$

$$= \frac{\partial}{\partial t}(A_i\rho\Delta x C T) \quad ( - )$$



$$\frac{\partial T}{\partial t} = -v \frac{\partial T}{\partial x} + \frac{1}{\tau_1}(T_w - T) \quad (A-2)$$

$$v \frac{\partial T}{\partial x} \quad \tau_1 = \frac{A_i\rho C}{\pi D_i h_i} [s]$$

(D)

( )

( )

$$f(v, \frac{\partial T}{\partial x}) = v \frac{\partial T}{\partial x} \cong (v - v_s) \frac{dT}{dx} + v_s \frac{\partial T}{\partial x} \quad (A-3)$$

(A-2) (A-3)

			IAE
	/	/	/
	/	/	/

( ) ( )

$$0 = -\nu_s \frac{dT_s}{dx} + \frac{1}{\tau_1}(T_{w_s} - T_s) \quad (\text{A-7})$$

$$0 = \frac{1}{\tau_2}(T_g - T_w) - \frac{1}{\tau_{12}}(T_w - T) \quad (\text{A-8})$$

$$c = \nu_s \tau_1 \left(1 + \frac{\tau_2}{\tau_{12}}\right) [m]$$

$$T_{S_0} = T_S(x=0) = T(x=0, t=0)$$

( ) ( ) ( ) ( )

$$\frac{\partial \delta T}{\partial t} = -\delta v \frac{dT_s}{dx} - \nu_s \frac{\partial \delta T}{\partial x} + \frac{1}{\tau_1}(\delta T_w - \delta T) \quad (\text{A-10})$$

$$\frac{\partial \delta T_w}{\partial t} = \frac{1}{\tau_2}(\delta T_g - \delta T_w) - \frac{1}{\tau_{12}}(\delta T_w - \delta T) \quad (\text{A-11})$$

$$\delta T = T - T_s, \quad \delta v = v - \nu_s, \quad \delta T_w = T_w - T_{w_s}$$

$$\delta T_g = T_g - T_{g_s}$$

$\overline{\delta T_g}$   $\overline{\delta T}$ ,  $\overline{\delta v}$ ,  $\overline{\delta T_w}$

$$s \overline{\delta T} = -\overline{\delta v} \frac{dT_s}{dx} - \nu_s \frac{\partial \overline{\delta T}}{\partial x} + \frac{1}{\tau_1}(\overline{\delta T_w} - \overline{\delta T}) \quad (\text{A-12})$$

$$s \overline{\delta T_w} = \frac{1}{\tau_2}(\overline{\delta T_g} - \overline{\delta T_w}) - \frac{1}{\tau_{12}}(\overline{\delta T_w} - \overline{\delta T}) \quad (\text{A-13})$$

$$: \quad (\text{A-13}) \quad (\text{A-12}) \quad \overline{\delta T_w}$$

$$\frac{d \overline{\delta T}}{dx} + \frac{a}{\nu_s} \overline{\delta T} = -\frac{\overline{\delta v}}{\nu_s} \frac{dT_s}{dx} + \frac{b}{\nu_s} \overline{\delta T_g} \quad (\text{A-14})$$

$$a(s) = s + \frac{1}{\tau_1} - \frac{\tau_2}{\tau_1(\tau_{12}\tau_2s + \tau_{12} + \tau_2)}$$

$$b(s) = \frac{\tau_{12}}{\tau_1(\tau_{12}\tau_2s + \tau_{12} + \tau_2)} \quad (\text{A-14})$$

$$: \quad x=0 \quad \overline{\delta T}(x, s) = \overline{\delta T}(0, s)$$

$$\overline{\delta T} e^{\frac{a}{\nu_s}x} = -\frac{\overline{\delta v}}{\nu_s} \int_0^x \frac{dT_s}{dx} e^{\frac{a}{\nu_s}x} dx \quad (\text{A-15})$$

$$+ \frac{b}{\nu_s} \overline{\delta T_g} \int_0^x e^{\frac{a}{\nu_s}x} dx + \overline{\delta T}(0, s)$$

$$dT_s \quad (\text{A-9})$$

$$\frac{\partial T}{\partial t} = -(\nu - \nu_s) \frac{dT_s}{dx} - \nu_s \frac{\partial T}{\partial x} + \frac{1}{\tau_1}(T_w - T) \quad (\text{A-4})$$

:  $\Delta x$

$$\pi D_o h_o \Delta x (T_g - T_w) - \pi D_i h_i \Delta x (T_w - T) = \quad (\text{A-5})$$

$$A_w \Delta x \rho_w C_w \frac{\partial T_w}{\partial t}$$

$$\frac{\partial T_w}{\partial t} = \frac{1}{\tau_2}(T_g - T_w) - \frac{1}{\tau_{12}}(T_w - T) \quad (\text{A-6})$$

$$\tau_{12} = \frac{A_w \rho_w C_w}{\pi D_i h_i} [s] \quad , \quad \tau_2 = \frac{A_w \rho_w C_w}{\pi D_o h_o} [s]$$

$l$		
$A_i$		$m^2$
$A_w$		$m^2$
$c$		$J / kg^\circ C$
$C_w$		$J / kg^\circ C$
$D_i$		$m$
$D_o$		$m$
$h_i$		$W / m^2^\circ C$
$h_o$		$W / m^2^\circ C$
$L$		$m$
$\rho$		$kg / m^3$
$\rho_w$		$kg / m^3$
$T(x, t)$		$^\circ C$
$T_g(t)$		$^\circ C$
$T_w(x, t)$		$^\circ C$
$\nu(t)$		$m / s$

---


$$\overline{\delta T} = -\overline{\delta v} \frac{T_{gs} - T_{S_0}}{ac - v_s} (e^{-\frac{x}{c}} - e^{-\frac{a}{v_s}x}) \quad (A-17) \quad \int_0^x \frac{dT_s}{dx} e^{\frac{a}{v_s}x} dx = \frac{T_{gs} - T_{S_0}}{a\tau_1(1 + \frac{\tau_2}{\tau_1}) - 1} (e^{\frac{x(a-\frac{1}{c})}{v_s}} - 1) \quad (A-16)$$

$$+ \overline{\delta T}_g \frac{b}{a} (1 - e^{-\frac{a}{v_s}x}) + \overline{\delta T}(0, s) e^{-\frac{a}{v_s}x} \quad (A-15)$$

∴

- 1 - Gay, D. H. and Ray, W. H. (1995). "Identification and control of distributed parameter systems by means of the singular value decomposition." *Chemical Engineering Science*, Vol. 50, No. 10, PP. 1519-1539.
  - 2 - Butkowskii, A. G. (1969). *Distributed Parameter Systems*, American Elsevier.
  - 3 - Ray, W. H. (1978). "Some recent applications of distributed parameter systems theory- a survey." *Automatica*, Vol. 14, No. 3, PP. 281-287.
  - 4 - Ramanathan, S., Curl R. L. and Kravaris, C. (1987). "Dynamics and control of the cumulative mass fraction of a particle size distribution." *ACC Proc.*, Minneapolis.
  - 5 - Ramanathan, S. (1988). *Control of Quasirational Distributed Systems with Examples on the Control of Cumulative Mass Fraction of Particle Size Distribution*, Ph.D Thesis, University of Michigan, Ann Arbor.
  - 6 - Ramanathan, S., Curl R. L. and Kravaris, C. (1989). "Dynamics and Control of Quasirational Systems." *AIChE J.*, Vol. 35, No.6, PP.1017-1028.
  - 7 - Özbay, H. (1993). "H $\infty$  optimal controller design for a class of distributed parameter systems." *International Journal of Control*, Vol.58, No.4, PP.739-782.
  - 8 - Foias, C., Özbay, H. and Tannenbaum, A. (1995). "Robust control of infinite dimensional systems-frequency domain methods." *Lecture Notes in Control and Information Sciences*, Vol.209.Berlin: Springer.
  - 9 - Toker, O. and Özbay, H. (1996). "On the rational H $\infty$  controller design for infinite dimensional plants." *International Journal of Robust and Non-linear Control*, Vol.6, No.5, PP.383-397.
  - 10 - Vollmer, U. and Raisch, J. (2001). "H $\infty$ -Control of a continuous crystallizer." *Control Engineering Practice*, Vol. 9, No. 8, PP. 837-845.
  - 11 - Zl'itek, P. and Hlava, J. (2001). "Anisochronic internal model control of time delay systems." *Control Engineering Practice*, Vol. 9, No. 5, PP. 501-516.
  - 12 - Vollmer U. and Raisch J. (2002). "Population balance modeling and H $\infty$ -Controller design for a crystallization process." *Chemical Engineering Science*, Vol. 57, No. 20, PP. 4401-4414.
  - 13 - Dimitri Breda. (2006). "Solution operator approximations for characteristic roots of delay differential equations." *Applied Numerical Mathematical*, Vol. 56, No. 3, PP. 305-317.
  - 14 - Verheyden, K., Luzyanina, T. and Roose, D. (2007). "Efficient computation of characteristic roots of delay differential equations using LMS methods." *J. Comput. Appl. Math*, Vol. 214, No. 1, PP. 209-226.
  - 15 - Bellman, R.E. and Cooke, K. L. (1963). *Differential-Difference Equations*, Chap. 12, Academic Press, New York.
  - 16 - Krall, A. M. (1967). *Stability Techniques for Linear Systems*, Chap. 7, Gordon and Breach, New York.
  - 17 - Manitius, A., Tran, H., Payre, G. and Roy, R. (1987). "Computation of eigenvalues associated with functional differential equations." *Siam J. Sci. Stat. Comput.*, Vol. 8, No. 3, PP. 222.
-

- 
- 18 - Shirvani, M., Inagaki, M. and Shimizu, T. (1993). "A simplified model of distributed parameter systems." *Int. J. Eng.*, Vol. 6, No. 2.PP. 65-78.
- 19 - Shirvani, M., Inagaki, M. and Shimizu, T. (1995). "Simplification study on dynamic models of distributed parameter systems." *AIChE J.*, Vol. 41, No. 12, PP. 2658-2660.
- 20 - Shirvani, M., Doustary, M. A., Shahbaz, M. and Eksiri, Z. (2004). "Heuristic process model simplification in frequency response domain." *I. J. E. Transactions B: Applications*, Vol. 17, No. 1, PP.19-39.
- 21 - Morari, M. and Zafiriou, E. (1989). *Robust Process Control*, Englewood Cliffs, NJ: Prentice-Hall.
- 22 - Cohen, W.C. and Johnston, E. F. (1956). "Dynamic characteristics of double-pipe heat exchangers." *Industrial and Engineering Chemistry*, Vol. 48, No. 6, PP. 1031-1034.
- 23 Romero, J. A., Campo, A. And Albertos, P. (2005). "Control of a heat exchanger using an iterative design approach." *16th IFAC World Congress*, Prague.

- 1 - Distributed Parameter Process  
2 - Robustness
-