

*

(// // //)

NP-hard

/ :

[]

n

m

(JIT)

[] []

[]

[] [] []

/

(ET_{max})

[]

/

[]

[]

ET_{max}

[]

[]

ET_{max}

[]

ET_{max}

[]

[]

[]

[]

[]

/

• [] []
 [] []
 • []
 • []
 /
 []

$$Pm || ET_{max}$$

[]

NP-hard

$$Pm || E_{max}$$

[]

()

[]

$$Pm || E_{max}$$

$$Pm || ET_{max}$$

$$Pm || ET_{max}$$

NP-hard

$$Pm || E_{max}$$

()

$$m \quad n \quad J = \{ \dots n \}$$

j

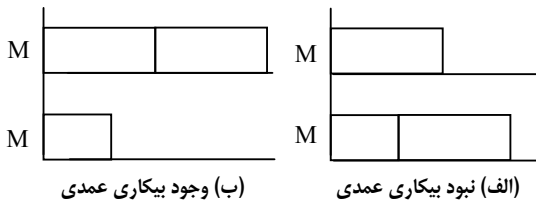
d_j

p_j

C_j

j

[]



شکل ۱: بررسی تأثیر تخصیص کارها در ایجاد بیکاری عمدی.

$$E_j = \max \{ d_j - C_j \} \quad ()$$

$$T_j = \max \{ C_j - d_j \} \quad ()$$

:

ET_{max}

$$ET_{max} = E_{max} + T_{max} \quad ()$$

T_{max}

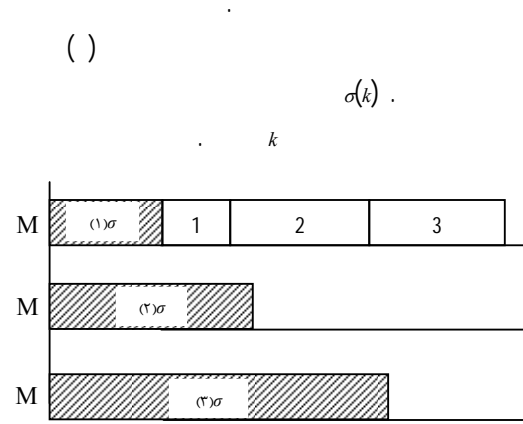
E_{max}

:

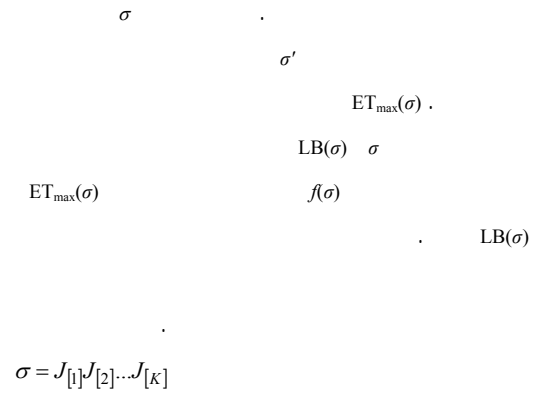
•

•

•



شکل ۲: نمایش نحوه محاسبه حد پایین زیر مسئله $Pm || E_{max}$



$Pm || T_{max}$

[]

$$C_{max}^* \leq C_m = \max\left(\frac{1}{m} \sum_{i \in \sigma} p_i, \max_{i \in \sigma} \{p_i\}, p_m + p_{m+1}\right) \quad ()$$

C_{max}^*

ET_{max}

LPT

$m+ \quad m$

(d_{max}) (C_m)

$L_{T_{max}} = \max(t_{min} + C_m - d_{max}, 0)$ ()

t_{min}

(σ)

σ

σ

$(Pm || T_{max})$ $(Pm || E_{max})$

NP-hard

[]

() NP-hard

9

$Pm || ET_{max}$

$Pm || E_{max}$

MST

$$\begin{matrix}
 \sigma & & j & i \\
 & & & \\
 & j & i & \\
 & & & \sigma_{ij} \\
 & & \sigma_{ji} & \\
 & & & [\quad] \quad \text{DYNA}
 \end{matrix}$$

لم ۱ (قاعده غلبه ۱) -

$$M \quad M$$

$$t_{M1} = t_{M2} \leq t_k \quad \forall k = 1, 2, \dots, m \quad ()$$

[]

$$\sigma_{ji} \quad \sigma_{ij}$$

T_{max}

E_{max}

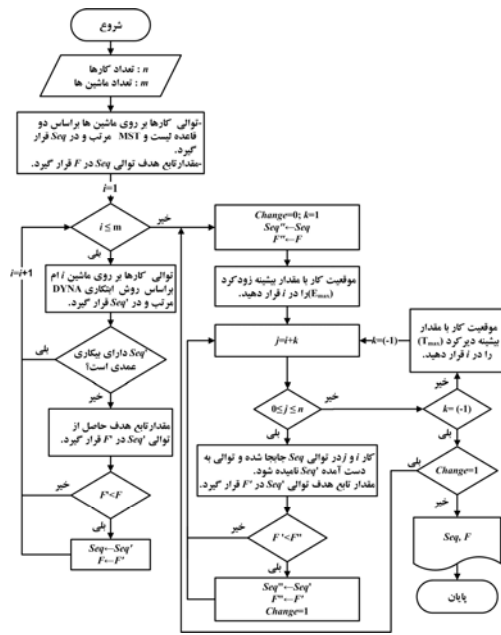
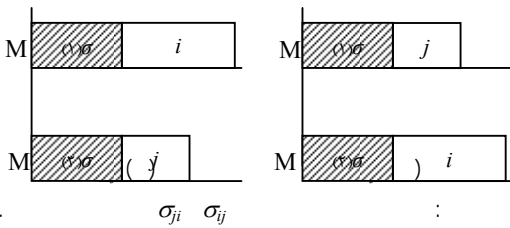
i

$$M \quad M$$

j

$$. ()$$

()



.MDP

[]

$$t \quad j \quad i$$

$$t_k + p_i + p_j \leq C_m - p_{\max} \quad ()$$

$$E_{\max}(ij) > E_{\max}(ji) \quad | \quad ET_{\max}$$

$$T_{\max}(ij) > T_{\max}(ji) \quad E_{\max}(ij) \geq E_{\max}(ji) \quad T_{\max}(ij) \geq T_{\max}(ji)$$

$$[] \quad ET_{\max}(\sigma_{ij}) \geq ET_{\max}(\sigma_{ji})$$

$$C_j \leq t_s \quad t_k + p_j \leq t_s \quad (ij) \quad j \quad i$$

$$[] \quad (ji)$$

$$\sigma_{ji} \quad p_i \geq p_j$$

$$t_k + p_i \leq t_s \quad j \quad i$$

$$\sigma_j$$

$$\sigma_{ji}$$

$$C_m - p_{\max}$$

$$C_m$$

$$C_m - p_{\max}$$

$$p_{\max}$$

$$[] \quad j \quad i$$

$$\sigma_{ji} \quad \sigma_j$$

$$k \quad ()$$

$$t_k \quad \sigma$$

$$m \quad j \quad i \quad \sigma$$

$$t_s \quad k$$

$$(\sigma_{ij}) \quad k \quad \sigma$$

$$() \quad () \quad ()$$

$$p_j \leq t_s - t_k \quad ()$$

$$p_j \leq p_i \quad ()$$

(

CYCLE PMX LOX

LOX

(GA)

[]

()

[]

() LOX

()

()

Pt:

۳	۷	۵	۸	۴	۶	۹	۱	۲
۳	H	۵	۸	۴	۶	H	۱	H
۳	۵	۸	H	H	H	۴	۶	۱

C₁:

۳	۵	۸	۲	۹	۷	۴	۶	۱
---	---	---	---	---	---	---	---	---

Pr:

۵	۶	۳	۲	۹	۷	۸	۱	۴
۵	H	۳	۲	۹	۷	H	۱	H
۵	۳	۲	H	H	H	۹	۷	۱

Cr:

۵	۳	۲	۸	۴	۶	۹	۷	۱
---	---	---	---	---	---	---	---	---

LOX

()

			...				
--	--	--	-----	--	--	--	--

MST EDD

()

۳	۷	۵	۸	۶	۹	۱
۳	۷	۹	۸	۶	۵	۱

کروموزوم اصلی

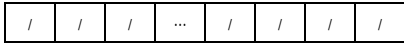
کروموزوم جهش یافته

[]

(PSO)

[]

()



D

[]

MST EDD

()

()

()

gbest

(

$$V_{i,t} = W_t \times V_{i,t-1} + C_1 \times Rand \times (P_i - X_{i,t-1}) + C_2 \times rand \times (P_g - X_{i,t-1}) \quad ()$$

[]

$$X_{i,t} = X_{i,t-1} + V_{i,t} \quad ()$$

i $X_{i,t}$ t i $V_{i,t}$

P_i t

P_g (pbest)

W (gbest)

g

P_i

c c []

$rand$ $Rand$

P_g

g

PSO

[,]

:

D

IV

C++

pbest

RAM

/

pbest

XP

gbest

gbest

[]

()

(τ)

[]

(R)

d_j

J_j

$[P(\tau R^l), P(\tau+R^l)]$

$$P = (1/m) \sum p_i$$

$\tau = | \quad R = | \quad \tau = | \quad R = | \quad \tau = | \quad R = |$

$\tau = | \quad R = |$

(*)

(* * =)

()

(* * =)

()

()

()

()

()

: () (ARE)

$$ARE = (1/k) \times \sum_{j=1}^k \frac{OPT_j - H_j}{OPT_j} \times$$

$H_j \quad OPT_j \quad k$

()

MDP

PSO GA

GA

PSO

g
 () g
 : (w_{max})
 : (w_{min})
 : (c) pbest
 : (c) gbest

PSO

PSO

میانگین درصد گره های قطع شده				میانگین		تعداد		ردیف		میانگین درصد گره های قطع شده				میانگین		تعداد		ردیف	
قاعده	قاعده	قاعده	حد	زمان حل	نمونه	m	n			قاعده	قاعده	قاعده	حد	زمان حل	نمونه	m	n		
غلبه ۳	غلبه ۲	غلبه ۱	پایین	(ثابته)	پهینه			غلبه ۳	غلبه ۲	غلبه ۱	پایین	(ثابته)	پهینه						
8.73	0.06	16.31	53.18	0.00	20	2	7	1	4.06	0.11	13.53	66.35	0.00	20	2	7	1		
3.29	0.07	34.82	44.48	0.00	20	3		2	0.77	0.11	38.60	43.80	0.00	20	3		2		
0.06	0.00	24.16	67.53	0.00	20	4		3	0.00	0.00	50.38	32.14	0.00	20	4		3		
0.00	0.00	18.25	75.56	0.00	20	5		4	0.00	0.00	57.12	23.86	0.00	20	5		4		
15.69	0.32	4.00	58.89	0.01	20	2	10	5	5.27	0.26	3.21	86.07	0.00	20	2	10	5		
4.29	0.30	23.05	56.75	0.00	20	3		6	5.48	0.00	23.06	54.57	0.00	20	3		6		
1.29	0.03	44.07	43.17	0.00	20	4		7	1.16	0.05	48.36	37.03	0.00	20	4		7		
0.36	0.01	40.35	50.02	0.00	20	5		8	0.04	0.01	64.22	22.35	0.00	20	5		8		
25.67	0.84	2.47	53.86	0.05	20	2	12	9	6.66	0.09	0.20	89.73	0.03	20	2	12	9		
13.58	0.25	7.68	60.74	0.07	20	3		10	7.76	0.07	16.08	63.45	0.04	20	3		10		
2.35	0.02	38.38	48.25	0.01	20	4		11	4.10	0.15	32.28	48.39	0.01	20	4		11		
0.46	0.04	35.08	57.47	0.01	20	5		12	0.63	0.00	56.98	30.99	0.01	20	5		12		
35.06	0.31	0.78	47.62	2.08	20	2	15	13	16.04	0.20	0.33	81.65	0.52	20	2	15	13		
18.20	0.50	5.64	60.27	3.47	20	3		14	9.28	0.10	16.28	66.08	0.41	20	3		14		
11.02	0.39	10.02	62.18	8.81	20	4		15	10.13	0.04	23.32	54.55	0.36	20	4		15		
3.04	0.35	23.17	63.91	0.54	20	5		16	2.92	0.17	41.11	43.85	0.46	20	5		16		
43.01	0.42	0.87	44.35	569.59	18	2	20	17	9.34	0.15	2.50	87.92	94.79	20	2	20	17		
31.23	0.49	1.71	52.95	1628.30	13	3		18	8.22	0.06	21.20	67.90	188.56	20	3		18		
20.94	0.42	2.37	63.41	760.93	17	4		19	16.40	0.23	24.71	52.65	65.84	20	4		19		
16.30	0.28	11.25	59.84	494.01	18	5		20	12.24	0.23	20.11	59.06	384.24	19	5		20		
54.66	0.46	0.89	36.70	3367.71	3	2	25	21	4.31	0.02	4.67	90.22	240.22	19	2	25	21		
39.07	0.47	1.65	48.09	3340.34	3	3		22	0.00	0.00	34.72	62.77	0.00	20	3		22		
27.26	0.46	2.79	59.16	3600.01	0	4		23	5.47	0.03	45.17	45.55	360.98	18	4		23		
24.17	0.38	3.52	61.55	3569.31	1	5		24	8.42	0.07	42.41	44.79	588.53	17	5		24		
1.71	0.00	12.99	72.52	0.00	20	2	7	1	1.32	0.16	15.22	66.77	0.00	20	2	7	1		
1.25	0.06	29.77	54.23	0.00	20	3		2	1.17	0.00	32.32	47.36	0.00	20	3		2		
0.56	0.00	42.49	41.64	0.00	20	4		3	0.31	0.00	43.61	39.36	0.00	20	4		3		
0.06	0.00	41.55	43.97	0.00	20	5		4	0.04	0.00	60.76	18.48	0.00	20	5		4		
5.77	0.15	10.62	67.74	0.00	20	2	10	5	5.52	0.11	11.74	66.18	0.00	20	2	10	5		
3.29	0.08	14.25	70.59	0.00	20	3		6	2.38	0.09	21.34	58.01	0.00	20	3		6		
1.13	0.03	17.35	74.22	0.00	20	4		7	0.69	0.11	40.01	41.02	0.01	20	4		7		
0.33	0.01	45.92	41.70	0.00	20	5		8	0.65	0.00	54.45	30.71	0.00	20	5		8		
11.66	0.03	5.30	69.33	0.01	20	2	12	9	9.42	0.18	2.63	69.13	0.03	20	2	12	9		
2.19	0.09	10.20	76.96	0.01	20	3		10	3.03	0.11	8.36	69.29	0.05	20	3		10		
1.45	0.02	14.11	77.22	0.00	20	4		11	1.41	0.15	24.03	53.49	0.06	20	4		11		
1.15	0.11	29.63	57.32	0.01	20	5		12	1.02	0.12	43.87	38.55	0.01	20	5		12		
11.94	0.04	2.19	74.81	0.11	20	2	15	13	11.44	0.05	1.87	71.08	0.81	20	2	15	13		
10.00	0.16	3.20	71.97	0.44	20	3		14	4.82	0.28	9.63	69.41	0.68	20	3		14		
3.37	0.11	7.57	77.45	0.60	20	4		15	3.57	0.24	5.31	69.10	1.05	20	4		15		
4.35	0.08	12.50	65.44	4.11	20	5		16	2.40	0.00	15.40	60.47	1.79	20	5		16		
18.28	0.20	0.91	68.33	75.53	20	2	20	17	13.85	0.09	0.93	72.49	326.75	19	2	20	17		
8.55	0.05	2.00	77.95	48.30	20	3		18	6.97	0.14	1.34	74.65	299.92	20	3		18		
6.84	0.10	5.81	69.38	122.99	20	4		19	4.38	0.07	3.40	73.74	877.70	17	4		19		
7.51	0.23	4.07	72.69	408.95	19	5		20	3.59	0.10	4.18	72.45	838.58	16	5		20		
17.43	0.11	0.59	69.49	1505.76	13	2	25	21	15.62	0.25	0.69	73.51	2013.19	12	2	25	21		
10.20	0.13	1.20	75.71	1842.43	11	3		22	13.32	0.11	1.30	68.89	3061.25	4	3		22		
8.97	0.12	1.96	73.32	2442.57	9	4		23	9.22	0.21	2.03	69.91	3114.78	3	4		23		
6.04	0.16	4.37	74.77	2182.50	10	5		24	3.14	0.22	6.73	72.00	2708.08	5	5		24		

NP-Hard

$$\begin{aligned}
 & : \\
 & () \quad , n, \dots, = \forall i \quad d_i = d = \\
 & : \\
 & () = C_{max}, C_r, C-d = \max (T_{max} = \max (\\
 & \quad C_{max} \quad T_{max} \\
 & \quad C_{max}
 \end{aligned}$$

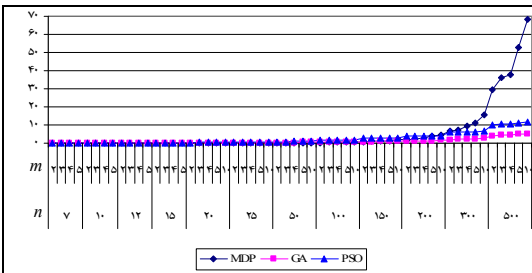
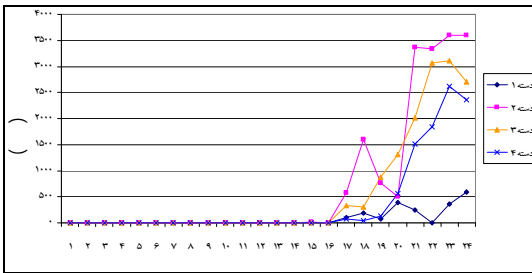
T_{max} [] NP-hard

NP-hard

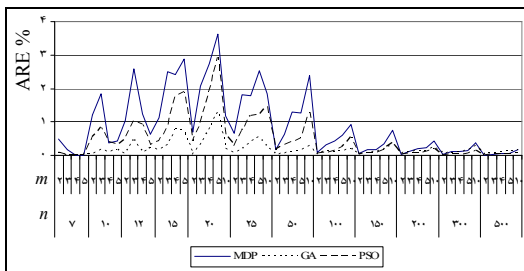
MDP

PSO GA

MDP



IEA



()

T_{max}

NP-

hard

-
- 1 - Baker, k.R. (1974). *Introduction to sequencing and scheduling*. John Wiley, New York.
 - 2 - Sidney, J.B. (1977). "Optimal single-machine scheduling with earliness and tardiness penalties." *Operations Research*, Vol. 25, No. 1, PP. 62-69.
 - 3 - Baker, K.R. and Scudder, G.D. (1990). "Sequencing with earliness and tardiness penalties: a review." *Operations Research*, Vol. 38, PP. 22–36.
 - 4 - Valente, J.M.S. and Alves, R.A.F.S. (2005). "Improved lower bounds for the early / tardy scheduling problem with no idle time." *Journal of the Operational Research Society*, Vol. 56, PP. 604-612.
 - 5 - Abdul-Razaq, T.S. and Potts, C.N. (1988). "Dynamic programming state-space relaxation for single machine scheduling." *Journal of the Operational Research Society*, Vol. 39, PP. 141–152.
 - 6 - Azizoglu, M., Kondakci, S. and Kirca, O. (1991). "Bicriteria scheduling problem involving total tardiness and total earliness penalties." *International Journal of Production Economics*, Vol. 23, PP. 17–24.
 - 7 - Almeida, M.T. and Centeno, M. (1998). "A composite heuristic for the single machine early–tardy job scheduling problem." *Computers & Operations Research*, Vol. 25, PP. 625–635.
 - 8 - Valente, J.M.S., and Alves, R.A.F.S. (2005). "Improved heuristics for the early / tardy scheduling problem with no idle time." *Computers & Operations Research*, Vol. 32, PP. 557–569.
 - 9 - M’Hallah, R. (2007). "Minimizing total earliness and tardiness on a single machine using a hybrid heuristic." *Computers & Operations Research*, Vol. 34, No. 10, PP. 3126-3142.
 - 10 - Amin-Nayeri, M.R. and Moslehi, G. (2000). "Optimal algorithm for single machine sequencing to minimize early/tardy cost." *ESTEGHLAL Journal of Engineering* (In Persian), Vol. 19, No. 1, PP. 35-48.
 - 11 - Moslehi, G., Mahnam, M., Amin-Nayeri, M. and Azaron, A. (2010). "A branch and bound algorithm to minimize the sum of maximum earliness and tardiness in single machine." *International Journal of Operational Research*, Vol. 8, No. 4, PP. 458-482.
 - 12 - Tavakkoli-Moghaddam, R., Moslehi, G., Vasei, M. and Azaron, A. (2005). "Optimal scheduling for a single machine to minimize the sum of maximum earliness and tardiness considering idle insert." *Applied Mathematics and Computation*, Vol. 167, No. 2, PP. 1430-1450.
 - 13 - Tavakkoli-Moghaddam, R., Moslehi, G., Vasei, M. and Azaron, A. (2006). "A branch-and-bound algorithm for a single machine sequencing to minimize the sum of maximum earliness and tardiness with idle insert." *Applied Mathematics and Computation*, Vol. 174, No. 1, PP. 388-408.
 - 14 - Mahnam, M. and moslehi, G. (2009). "A branch and bound algorithm for minimizing the sum of maximum earliness and tardiness with unequal release times." *Engineering Optimization*, Vol. 41, No. 6, PP. 521-536.
 - 15 - Nekoimehr, N. and Moslehi, G. (in press). "Minimizing the sum of maximum earliness and maximum tardiness in the single-machine scheduling problem with sequence-dependent setup time." *Journal of the Operational Research Society*.
 - 16 - Lam, K. and Xing, K.W. (1997). "New trends in parallel machine scheduling." *International Journal of Operations & Production Management*, Vol. 17, No. 3, PP. 326-338.
 - 17 - Mokotoff, E. (2001). "Parallel machine scheduling problems: A survey." *Asia-Pacific Journal of Operational Research*, Vol. 18, No. 2, PP. 193-242.
 - 18 - Heady, R.B. and Zhu, Z. (1998). "Minimizing the sum of job earliness and tardiness in a multi-machine system." *International Journal of Production Research*, Vol. 36, PP. 1619–1632.
-

-
- 19 - Azizoglu, M. and Kirca, O. (1998). "Tardiness minimization on parallel machines." *International Journal of Production Economics*, Vol. 55, No. 2, PP. 163-168.
- 20- Balakrishnan, N., Kanet, J.J. and Sridharan, S.V. (1999). "Early/tardy scheduling with sequence dependant setups on uniform parallel machines." *Computers and Operations Research*, Vol. 26, PP. 127-141.
- 21 - Zhu, Z. and Heady, R.B. (2000). "Minimizing the sum of earliness/tardiness in multi-machine scheduling: a mixed integer programming approach." *Computers and Industrial Engineering*, Vol. 38, PP. 297-305.
- 22 - Ventura, J.A. and Kim, D. (2003) "Parallel machine scheduling with earliness-tardiness penalties and additional resource constraints." *Computers & Operations Research*, Vol. 30, PP. 1945-1958.
- 23 - Kedad-Sidhoum, S., Rios Solis, Y. and Sourd, F. (2008). "Lower bounds for the earliness-tardiness scheduling problem on parallel machines with distinct due dates." *European Journal of Operational Research*, Vol. 189, No. 3, PP. 1305-1316.
- 24 - Tavakkoli-Moghaddam, R., Jolai, F., Khodadadeghan Y. and Haghnevis, M. (2006). "A mathematical model of a multi-criteria parallel machine scheduling problem: A genetic algorithm", *International Journal of Engineering*, Vol. 19, No. 1, PP. 79-86.
- 25 - Tavakkoli-Moghaddam, R., Jolai, F. and Ghandi-Bidgoli, S. (2008). "A parallel machine scheduling problem minimizing the total weighted earliness and total weighted tardiness by a multi-objective scatter search method." *Journal of Faculty of Engineering -University of Tehran*, Vol. 42, No. 7, PP. 923-934.
- 26 - Jolai, F., Tavakkoli-Moghaddam, R. and Azadian, F. (2006). " Parallel machine scheduling for split jobs with sequence dependent setup times." *Journal of Faculty of Engineering (University of Tehran)*, Vol. 40, No. 4, PP. 495-506.
- 27 - Mandel, M. and Mosheiov, G. (2001). "Minimizing maximum earliness on parallel identical machines." *Computers and Operations Research*, Vol. 28, PP. 317-327.
- 28 - Fatemi Ghomi, S.M.T. and Jolai Ghazvini, F. (1998). "A pairwise interchange algorithm for parallel machine scheduling." *Production Planning & Control*, Vol. 9, No. 7, PP. 685-689.
- 29 - Holland, J.H. (1975). *Adaptation in Natural and Artificial Systems: An Introductory Analysis with Applications to Biology, Control, and Artificial Intelligence*. Ann Arbor, MI: University of Michigan Press.
- 30 - Goldberg, D.E. (1989). *Genetic algorithms in search, optimization, and machine learning*. Addison-Wesley.
- 31 - Eberhart, R. and Kennedy, J. (1995). "A new optimizer using particle swarm theory." *Proceedings of the 6th international symposium on micro machine and human science*, PP. 39-43.
- 32 - Hu, X., Shi, Y. and Eberhart, R., (2004). "Recent advances in particle swarm." *Proceedings of the IEEE Congress on Evolutionary Computation*. PP. 90-97.
- 33 - Kennedy, J. and Mendes, R. (2002). "Population structure and particle swarm performance." *Proceedings of the IEEE Congress on Evolutionary Computation*.
- 34 - Garey, M.R. and Johnson, D.S. (1978). "Strong NP-completeness results: motivation, examples, and implications." *J. Assoc. Comp. Mach*, Vol. 25, PP. 499-508.
-

-
- 1- Just inTime
 - 2- Identical
 - 3- Uniform
 - 4- Unrelated
 - 5- Minsum
 - 6- Minmax
 - 7- Forward
 - 8- Depth First
 - 9- Polynomial Time Algorithm
 - 10- Longest Processing Time
 - 11- MST-DYNA–Pairwise Interchange
 - 12- Permutation Based Approach
 - 13- Priority Based Approach
 - 14- Genetic Algorithm
 - 15- Roulette Wheel
 - 16- Elitist Strategy
 - 17- Linear Order Crossover Swap
 - 18- Partially Mapped Crossover
 - 19- Swap Mutation
 - 20- Particle Swarm Optimization
 - 21- Particle
 - 22- Swarm
 - 23- Average Relative Error
-